

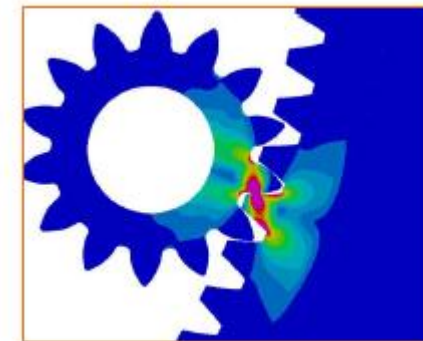
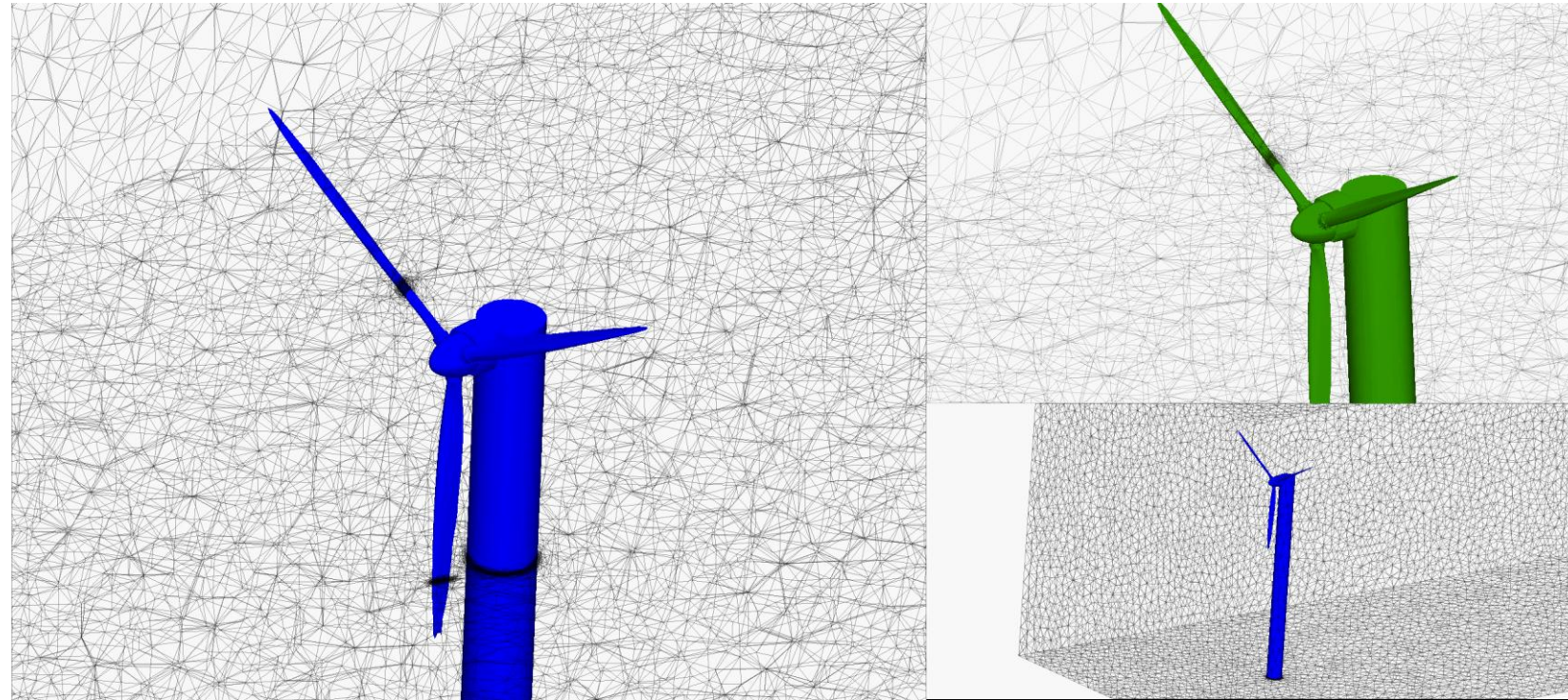
Industry 4.0: Challenges and opportunities for HPC and data-intensive applications

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MINES PARISTECH, PSL UNIVERSITY

Motivation : Industry 4.0



CAE: Computer Aided Engineering

- ❑ **Context**
- ❑ **Advanced Numerical Methods for CFD**
- ❑ **HPC and Big Data/AI Convergence**
- ❑ **Adaptive Algorithms based Error Estimation**
- ❑ **Conclusions**

Applied Maths, High Performance Computing (HPC) and Fluid Modeling

Elie Hachem

HDR 2014

Finite elements
and Fluid-Structure
Interaction



Youssef Mesri

HDR 2016

Finite elements, HPC &
meshing



Rudy Valette

HDR 2014

Rheology & complex
fluids



Thierry Coupez

HDR 2000

Finite elements and
fluids



Philippe Meliga

HDR 2018 – CNRS

Instabilities & control



RMP, SP2, TMP, CSM,...

Cemef



PERSEE, CDM, CES, CTP, CRC et
GeoSciences

ESPCI et IPGG (PSL)
INPHYNI, OCA, INRIA (UCA)



Stanford University, FRG
CIMNE UPC
DAMPT Cambridge
Barcelona SuperComputing
M2P2 Aix Marseille





□ Anisotropic and parallel 3D mesh adaptation

- A priori and a posteriori error estimators
- Boundary layers & multicriteria adaptation
- Conservative Interpolation

□ Advanced Finite elements methods

- Adaptive & monolithic framework
- Multi-scale approach VMS
- Conservative Levelset methods

□ Massively parallel computing

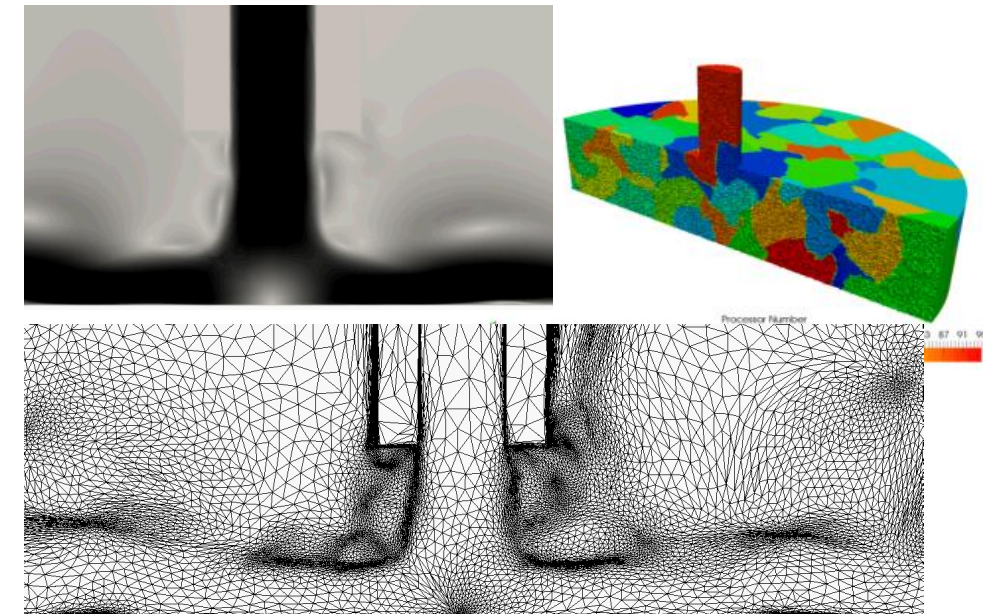
- Hierarchical mesh/domain decomposition
- Load balancing

□ Immersive methods

- Fluid-Structure Interaction
- Immersed domains: surface mesh & NURBS
- Extension to moving domains.

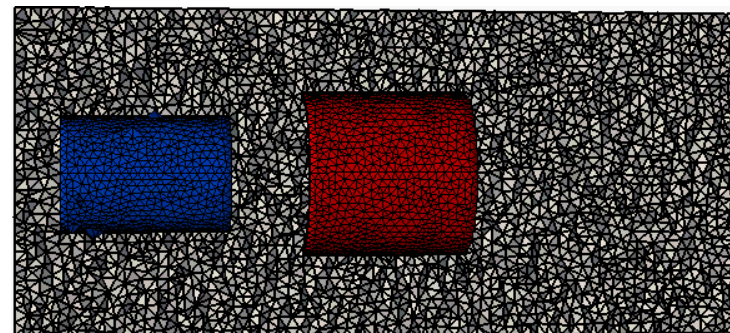
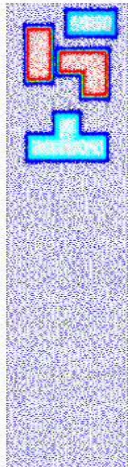
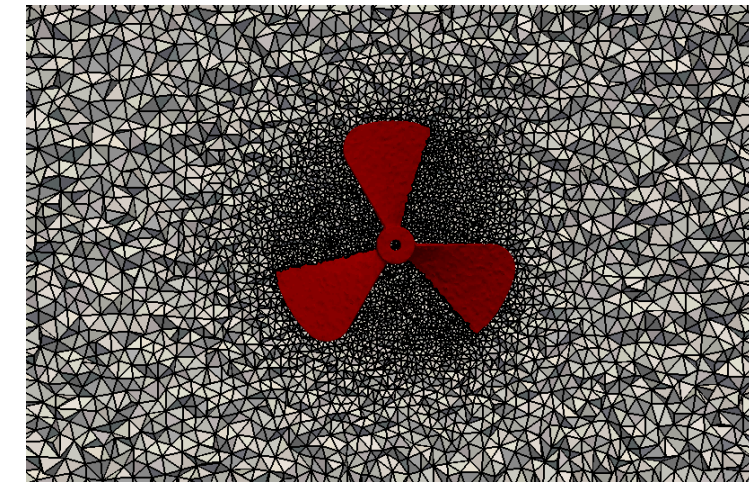
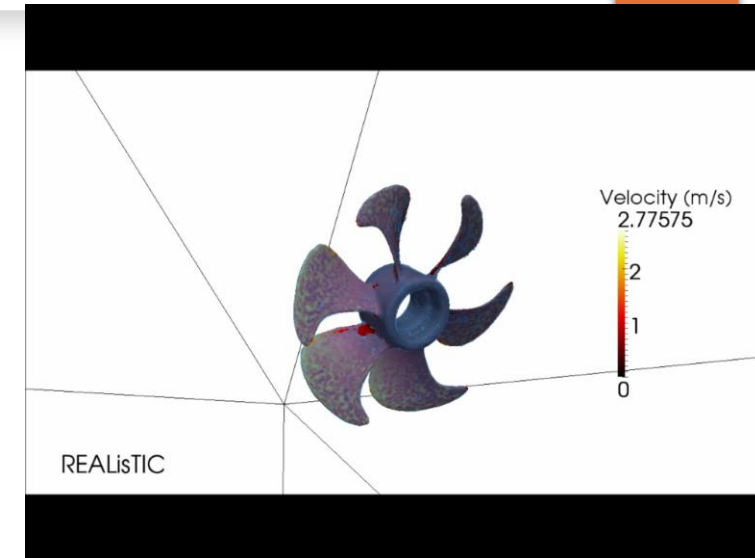


Experimental and numerical characterization of dense suspensions

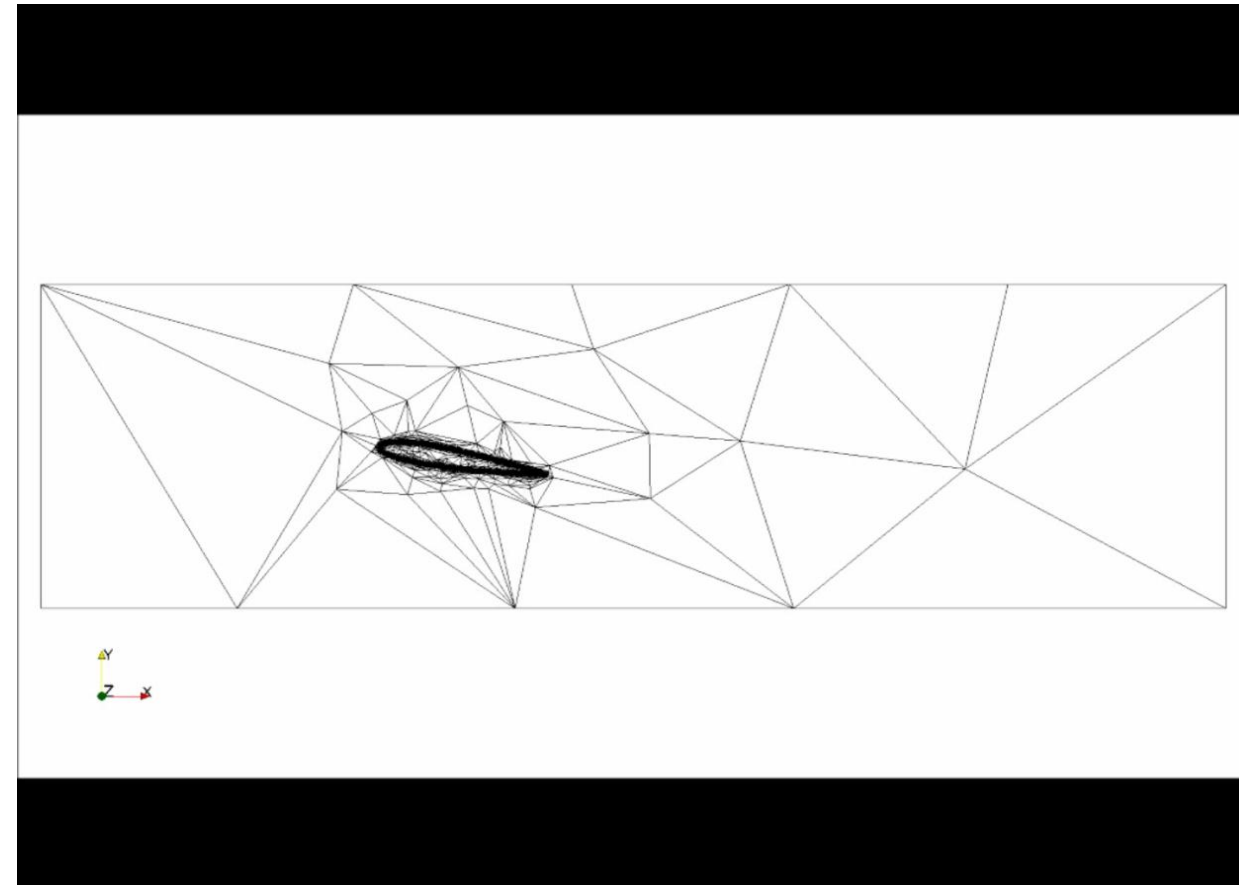
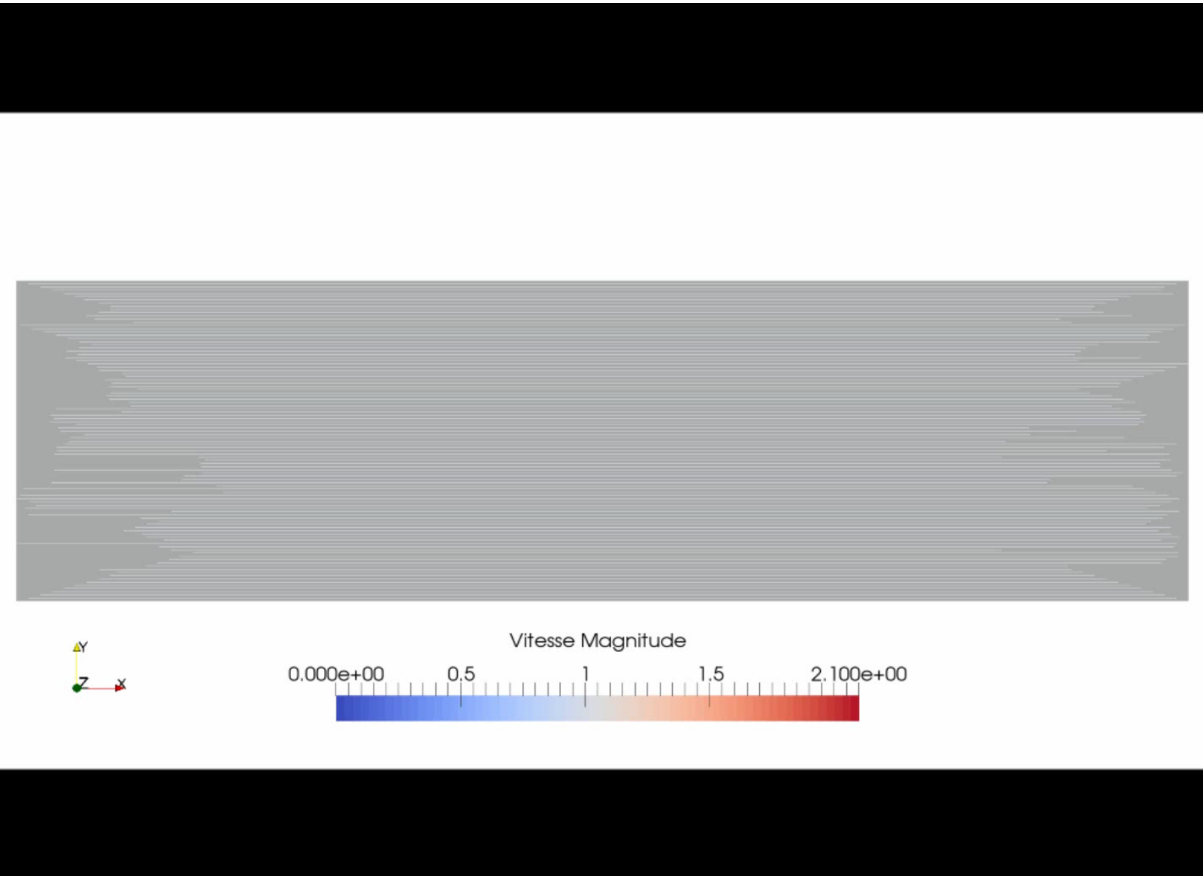


Impingement jet cooling

- ❑ **Anisotropic large mesh deformation**
 - Inverse Weighting Distance
 - Mesh quality-based approach
 - Conservative a priori geometric features (i.e. boundary layers, ...)
- ❑ **Multi-body configurations**
 - Adaptive & monolithic framework
 - Multi-scale approach VMS (iLES)
- ❑ **Massively parallel computing**
 - Hierarchical algorithms
 - Load balancing

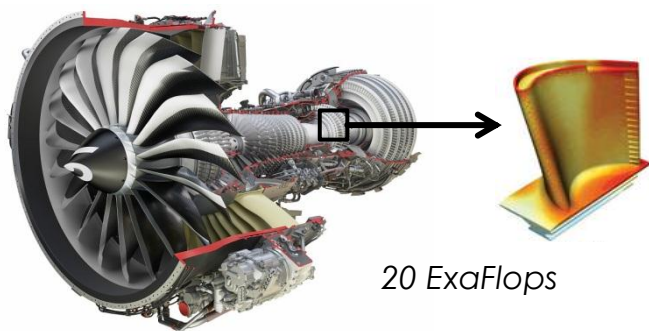


Turbulent incompressible Navier-Stokes flow

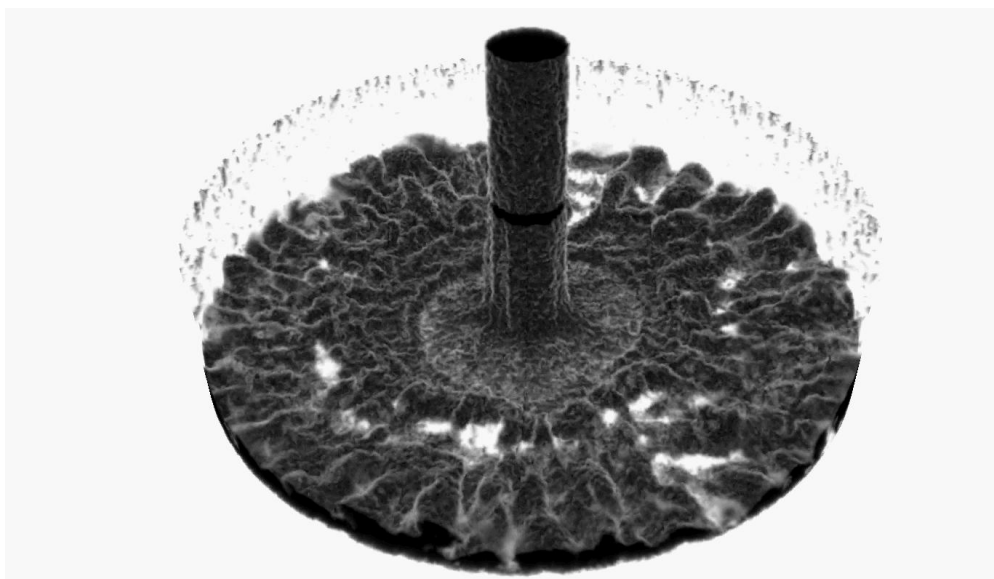


Vortex-Induced Vibration

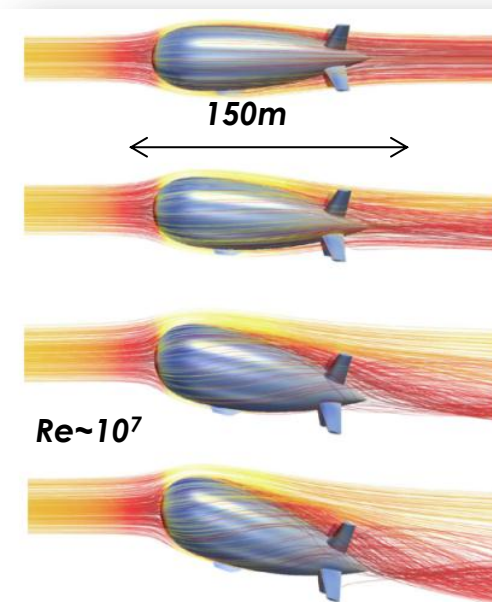
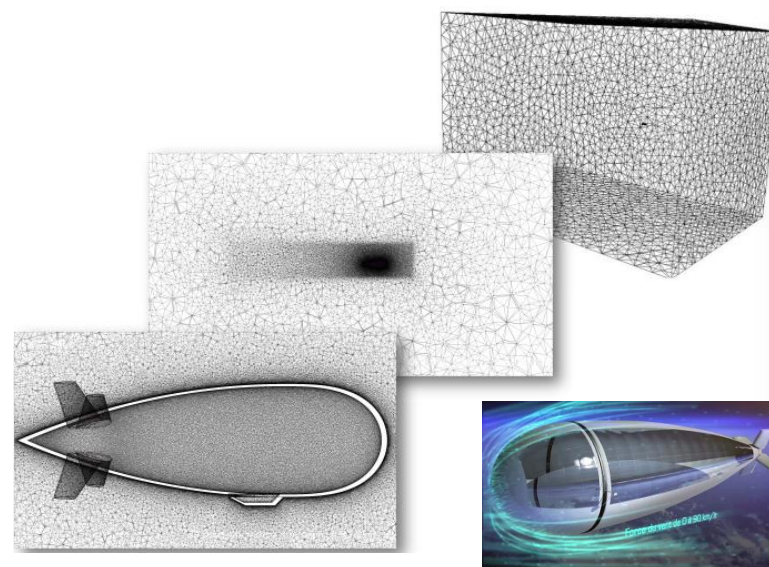
Challenge 1: Reduce environment impact of the civil aviation



20 ExaFlops



Challenge 2: Design of new stratospheric platforms



Industrial Chair:



Title: « Multi-scale digital framework for safety design of industrial quenching processes »

12 industrial partners

Period: 2018 – 2022

Site web: www.chaireinfinity.fr



Design of new high-quality material products

Extract useful information from large data set to perform efficiently large scale simulations

▶ Convergence between:

▶ Models

▶ High performance simulation algorithms and data analytics

HPC

Parallelism for scalability

Big Data

- ▶ Performance comes first
- ▶ Low level programming (MPI+X)
- ▶ Thin Software stack
- ▶ Stable software libs
- ▶ HPC centers

- ▶ Jobs runs few hours on thousands of cores

- ▶ Ease of programming comes first
- ▶ High level programming (Spark, TensorfFlow)
- ▶ Thick software stack
- ▶ Quickly changing libs
- ▶ Cloud platforms

- ▶ Jobs runs few days on tens of nodes

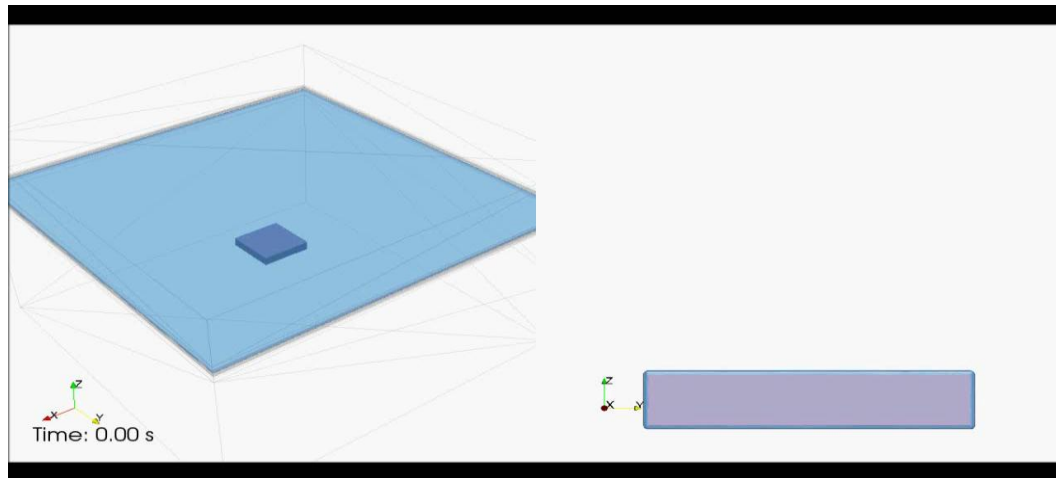
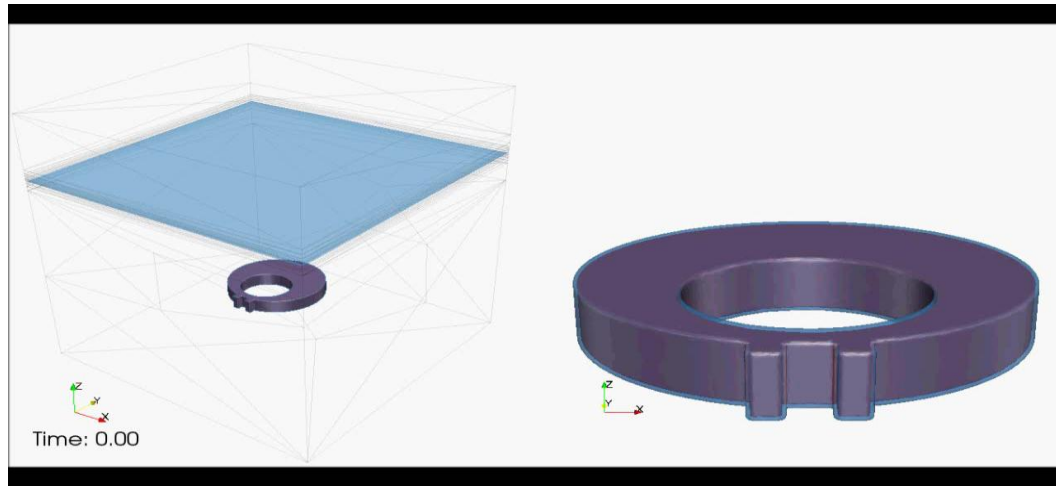
HPC and BigData/AI Convergence

Two research directions

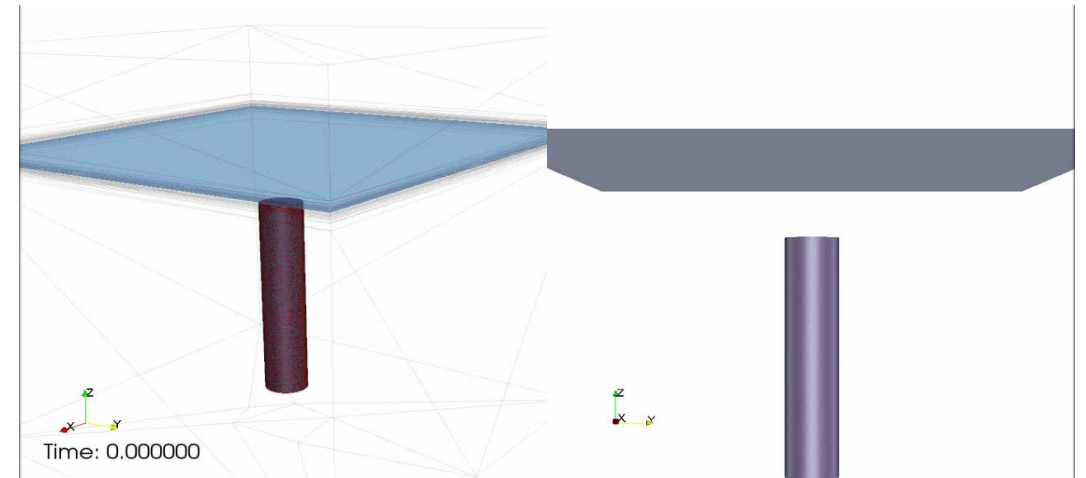
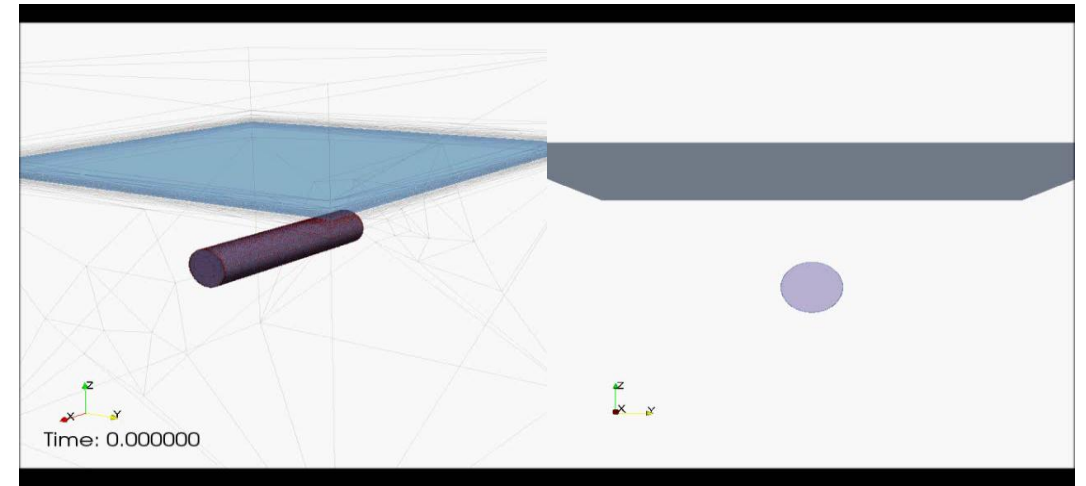
- ▶ Accelerating AI and Big Data with the help of HPC
 - ▶ Accelerating ML/DL with task-based programming (Dask, StarPU)
- ▶ AI/Big Data analytics for large scale scientific simulations
 - ▶ Large scale parallel deep reinforcement learning (Turbulence models, optimization,...)

Fast decision-making Tool - deep reinforcement learning

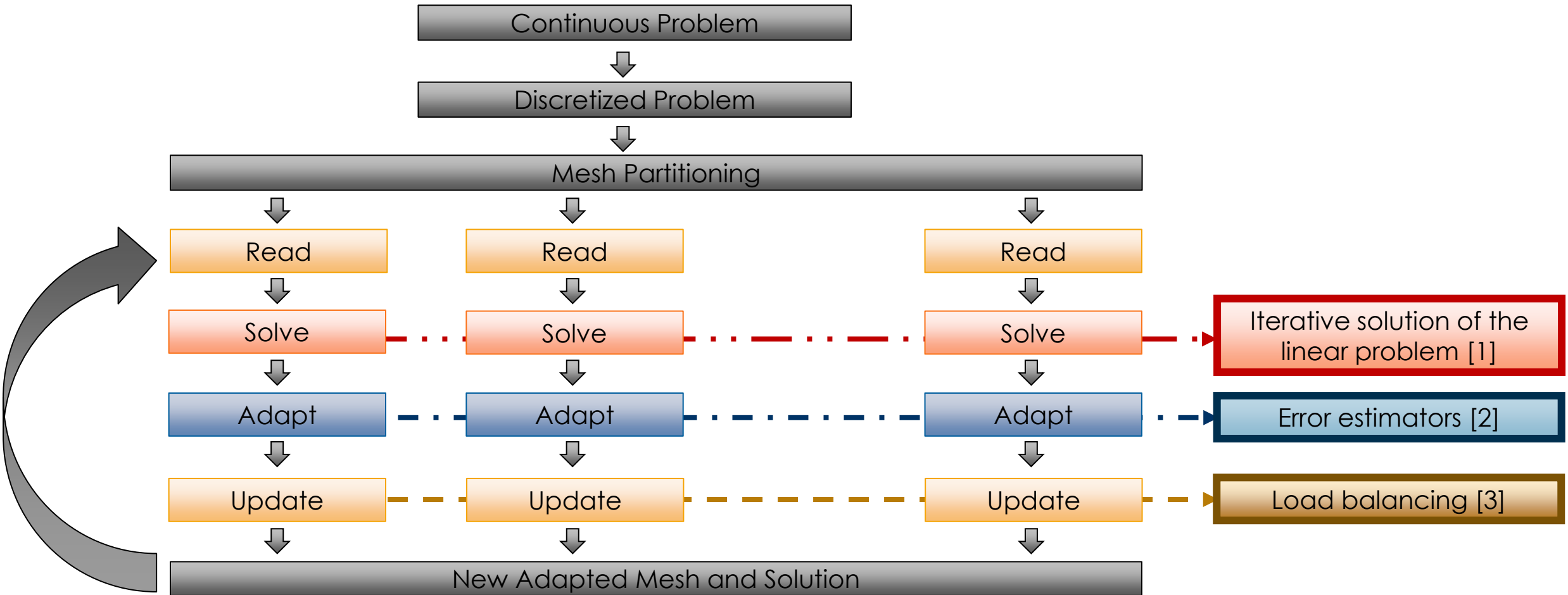
Geometry effect



Orientation effect



Parallel Adaptive Finite Element Framework

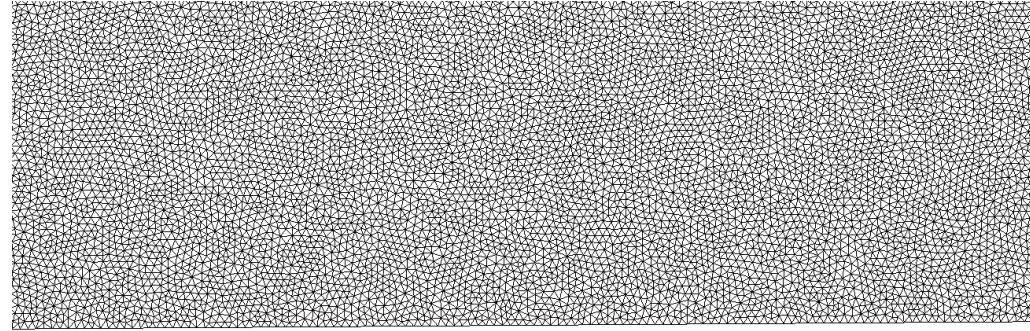


[1] G. Manzinali, E. Hachem, Y. Mesri, Adaptive stopping criterion for iterative linear solvers combined with anisotropic mesh adaptations, CMAME, 2018

[2] Bazile, A., Hachem, E., Larroya-Huguet, J. C., Mesri, Y. Variational Multiscale error estimator for anisotropic adaptive fluid mechanics simulations. CMAME, 331, 94-115, 2018.

[3] Y. Mesri, Predictive load balancing for parallel anisotropic mesh adaptation applications, preprint, 2018

Anisotropic and dynamic mesh adaptation



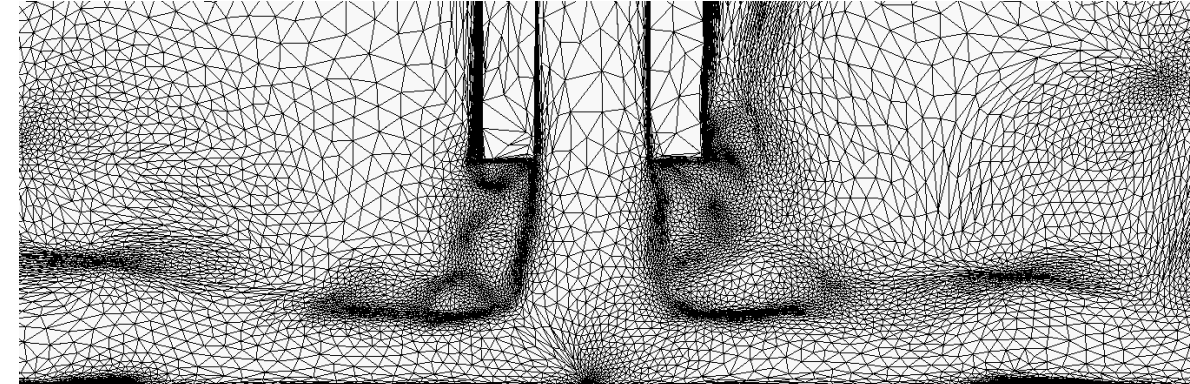
Modify the mesh anisotropically and dynamically according to a criteria.

add,
remove,
stretch cells.

along a
certain
direction

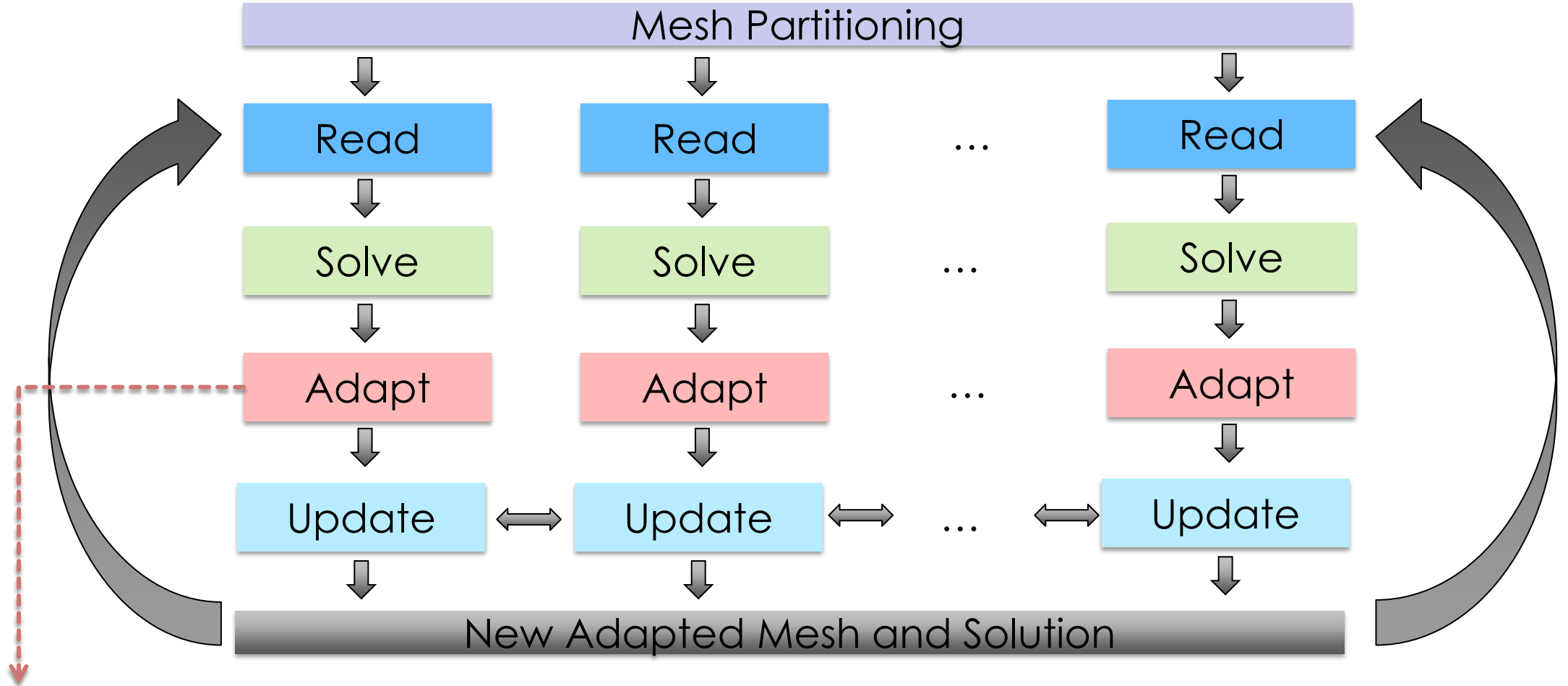
in the course of
time

via an error estimation,
or the solution's variation.



Dynamic anisotropic mesh according to velocity variations: velocity field (left), adapted mesh (right).

Dynamic and parallel mesh adaptation algorithm



Adapt:

1. **Estimate the error at each iteration step.**
2. Correlate the error with the mesh geometry.
3. Generate a new mesh in the metric space.

Error Indicator:

$$\eta_{\Omega_e} = d|\Omega_e|^{\frac{1}{p}} |\lambda_d(x_0)| h_d^2$$

Interpolation error estimator:

- ▶ d the dimension of the problem,
- ▶ λ_d the eigenvalue of the recovered Hessian matrix $H_R(u)(x)$,
- ▶ h_d the size of the element in the direction d .

$$\|u - u_h\|_{L^p(\Omega)} \leq C \|u - \Pi u\|_{L^p(\Omega)}$$



$$\bar{\eta}_T^p = \int_T (\mathcal{H}(u_h(x_T))(x - x_T) \cdot (x - x_T))^p dT$$

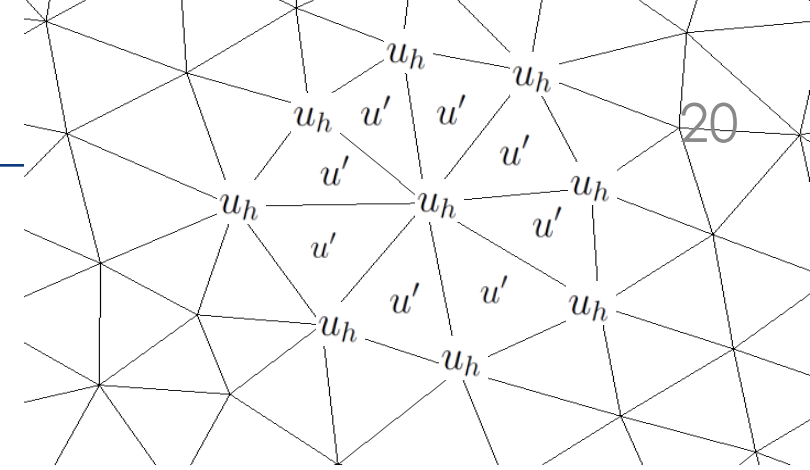
Anisotropic metric definition:

$$\mathcal{H} = \mathcal{R} \Lambda \mathcal{R}^T = |\lambda_1| e_1 \otimes e_1 + \dots + |\lambda_d| e_d \otimes e_d$$

$$\left\{ \begin{array}{l} \text{Find } h_T = \{h_{1T}, \dots, h_{dT}\}, T \in \mathcal{T}_h \text{ that minimizes the cost function} \\ F(h_T) = \sum_{T \in \mathcal{T}_h} (\eta_T)^p \\ \text{under the constraint } N_{\mathcal{T}_h'} = C_0^{-1} \sum_{T \in \mathcal{T}_h} \int_T \prod_{i=1}^d \frac{1}{h_{iT}} dT \end{array} \right.$$

➤ Modification of the mesh according to this geometrical transformation.

Type 2: A posteriori subscales error estimator



A posteriori subscales error estimator:

$$\|u'\|_{L^\infty(\Omega)}$$

Variational Multi Scale framework: $u = u_h + u'$ $u_h \in \mathcal{S}_h, u' \in \mathcal{S}'$

resolved part (coarse scales)

unresolved part (subscales) $\approx Error$

Two contribution to the error:

$$u'(\mathbf{x}) = u'_{bub}(\mathbf{x}) + u'_{poll}(\mathbf{x})$$

Internal residual error
(inside the element)

Inter-element error
(outside the element)

❖ negligible for convective-dominated heat transfer

We obtain an explicit expression of the error:

$$u'(\mathbf{x}) \approx u'_{bub}(\mathbf{x}) = \sum_{i=1}^{n_{bub}} c_i^b b_i(\mathbf{x})$$

Irisarri, D., & Hauke, G. (2017). Pointwise Error Estimation for the One-Dimensional Transport Equation Based on the Variational Multiscale Method. *IJCM*, 14(04), 1750040.

- We compute explicitly the a posteriori subscales error estimator.

New isotropic metric based mesh adaptation:

We propose the following **new isotropic metric tensor**:

$$\mathcal{H}_{iso} = \mathcal{R}\Lambda\mathcal{R}^T = |\lambda|e_1 \otimes e_1 + \dots + |\lambda|e_d \otimes e_d$$

With:

$$|\lambda| = \frac{1}{h_{new}^2} = \frac{\|u'\|_{L^\infty(\Omega_e)}}{u'_{TOL}} \times \frac{1}{h^2}$$

Where \mathcal{R} is the orthogonal matrix built with eigenvectors $(e_i)_{\{i=1,\dots,d\}}$ of $H_R(u_h(x))$

New anisotropic metric based mesh adaptation:

We propose a **new anisotropic local error indicator**:

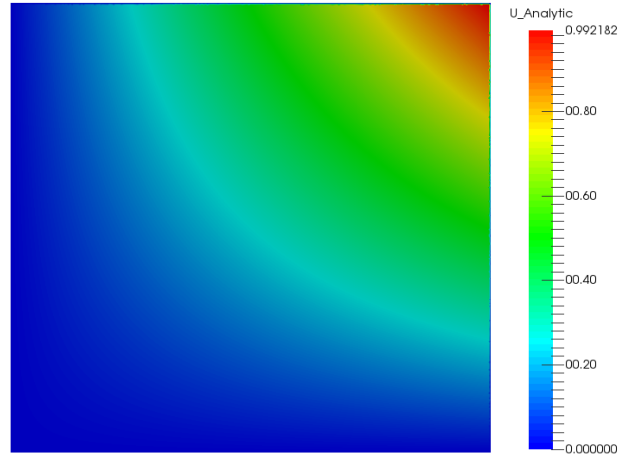
With

$$\eta_{\Omega_e,new} = d|\Omega_e|^{\frac{1}{p}} \times |\lambda_d(x_0)| \times \frac{\|u'\|_{L^\infty(\Omega_e)}}{u'_{TOL}} \times h_{d,new}^2$$

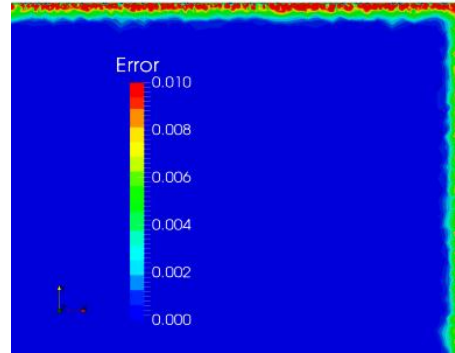
$$\mathcal{H}_{aniso}^{new} = \mathcal{R}\Lambda\mathcal{R}^T = \frac{\|u'\|_{L^\infty(\Omega_e)}}{u'_{TOL}} |\lambda_1|e_1 \otimes e_1 + \dots + \frac{\|u'\|_{L^\infty(\Omega_e)}}{u'_{TOL}} |\lambda_d|e_d \otimes e_d$$

Where \mathcal{R} is the orthogonal matrix built with eigenvectors $(e_i)_{\{i=1,\dots,d\}}$ of $H_R(u_h(x))$

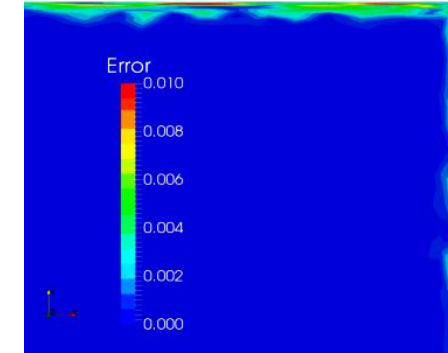
Numerical example in 2D:



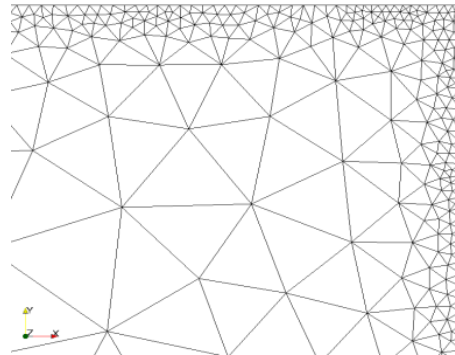
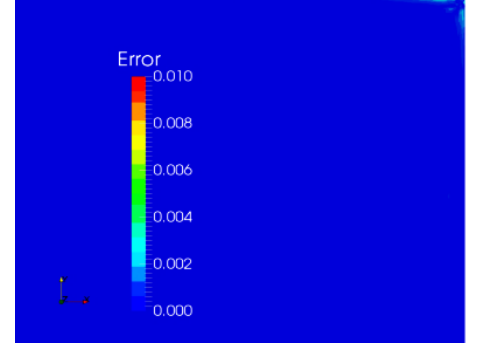
Isotropic mesh 2



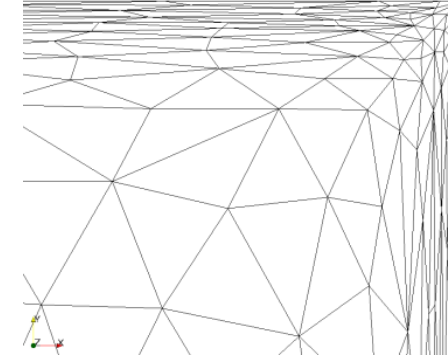
Anisotropic mesh 1



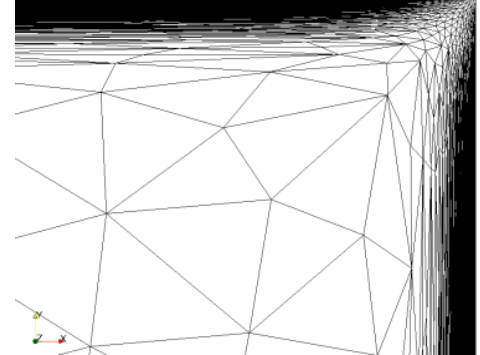
Anisotropic mesh 3



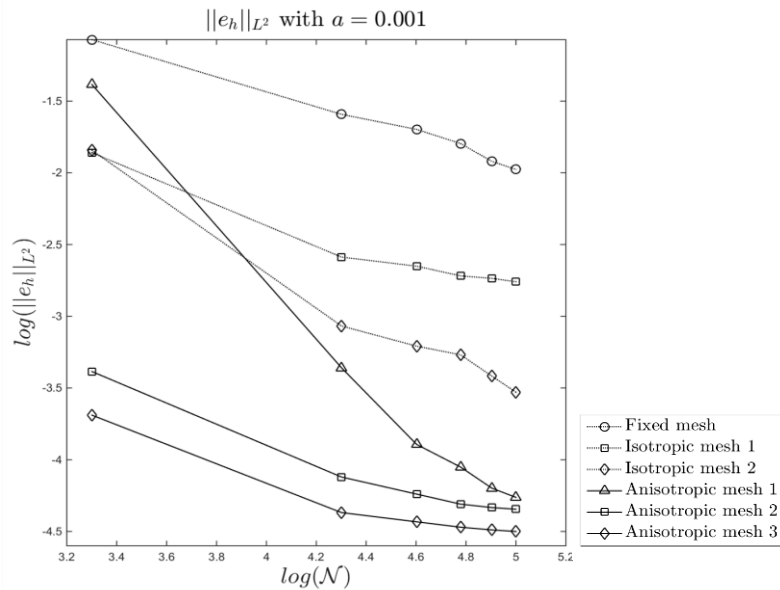
$N = 20\,798$



$N = 20\,932$



$N = 23\,182$



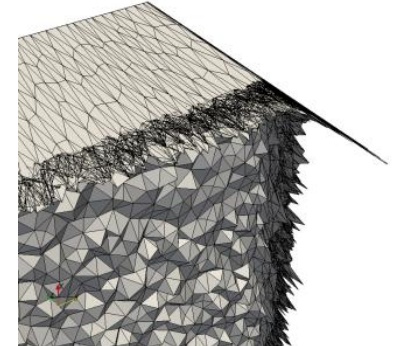
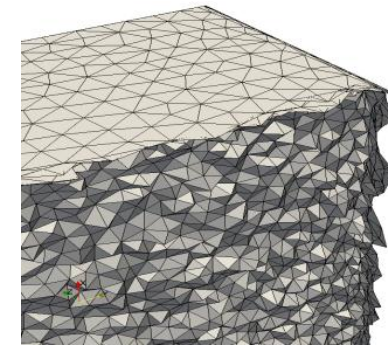
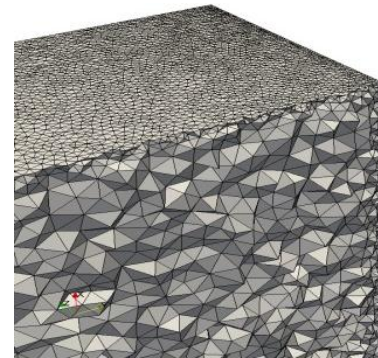
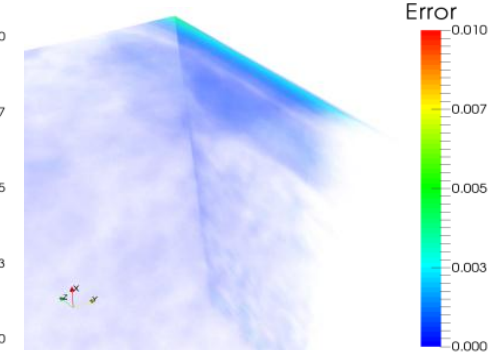
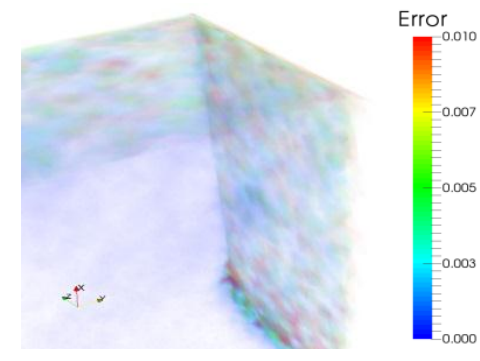
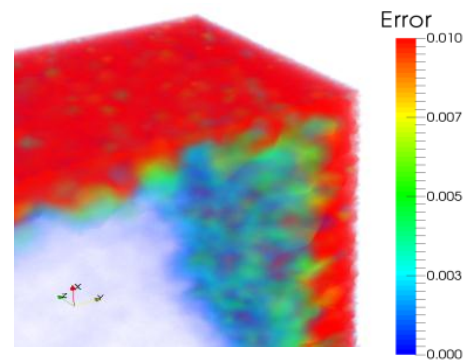
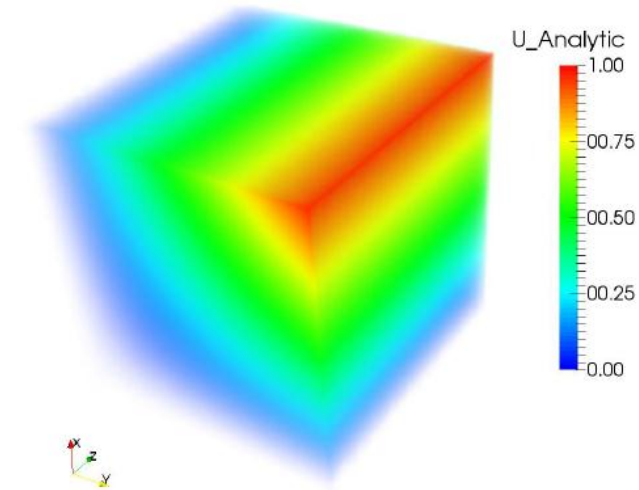
Numerical benchmarks with analytical solutions

Numerical example in 3D:

Isotropic mesh 2

Anisotropic mesh 1

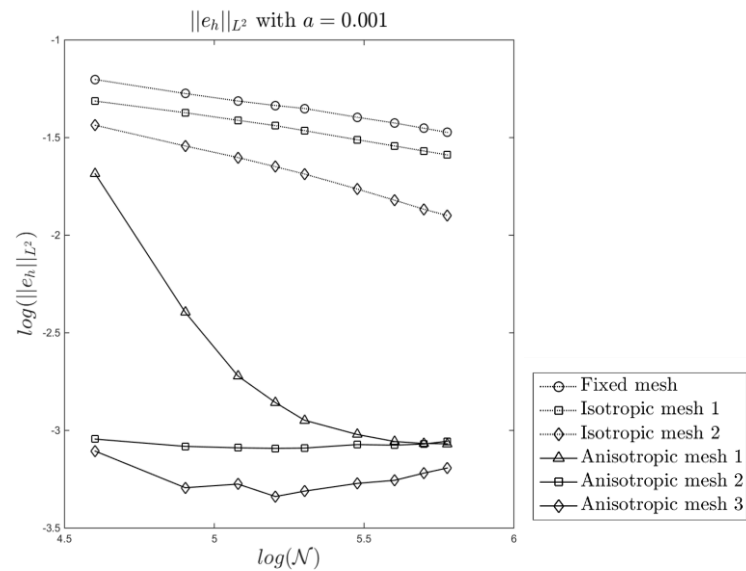
Anisotropic mesh 3



$N = 198\,946$

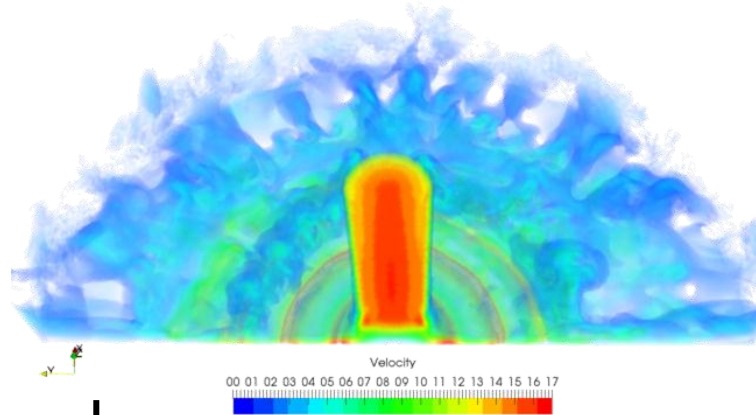
$N = 212\,242$

$N = 199\,659$

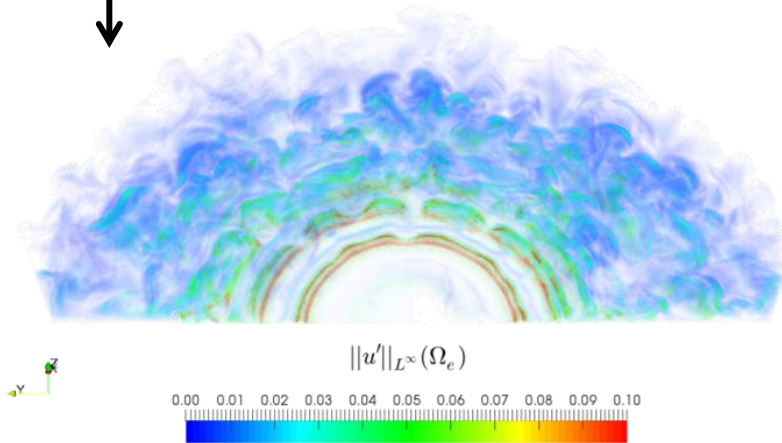


Application to the impingement jet cooling

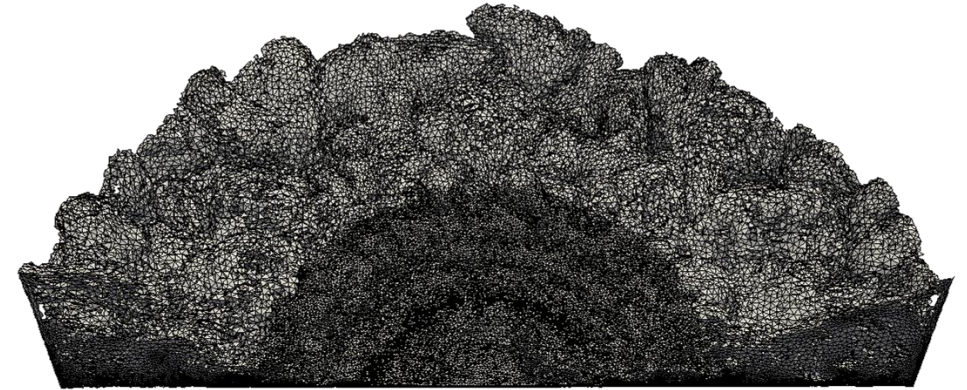
Capturing the thermal activity due to the secondary vortexes with the new anisotropic mesh adaptation based on the subscales error estimator.



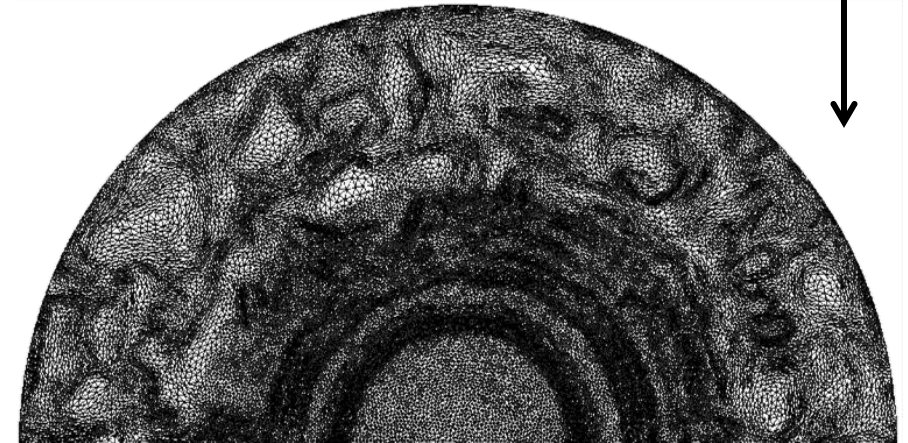
Velocity field:



A posteriori subscales error estimate:



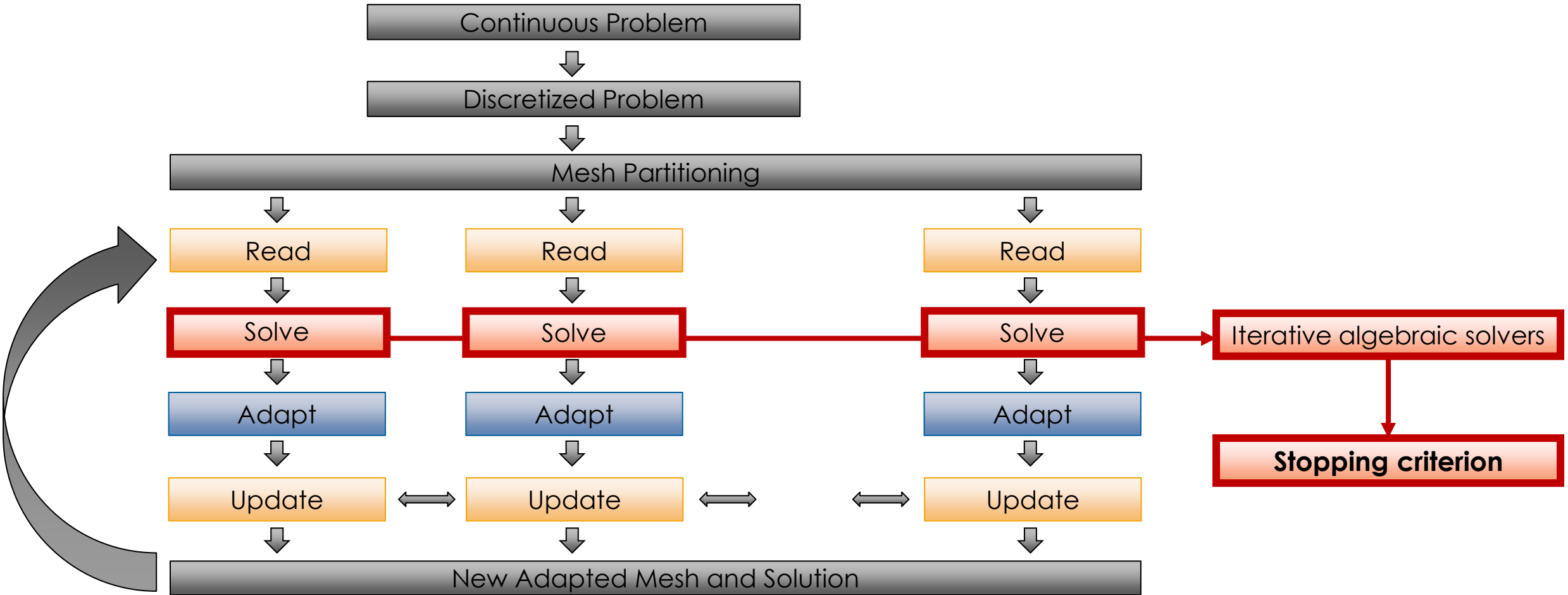
Multiscale adapted mesh (using $\eta_{\Omega_e, new}$):



Slice view on plan XY at z=0

Adaptive Stopping Criteria for Iterative Solvers

AFEM framework – Adaptive Stopping Criterion



Adaptive stopping criterion – Error estimate based

The main idea is to **stop** the iterative resolution when the **algebraic error** is lower than to the **estimated error**

$$\|\nabla(u_h - u_h^n)\|_{L^2} \leq c \left(\sum_{T \in \mathcal{T}_h} \eta_T^2 \right)^{1/2}$$

Assumptions

- **Algebraic error** approximated to the **residual error**

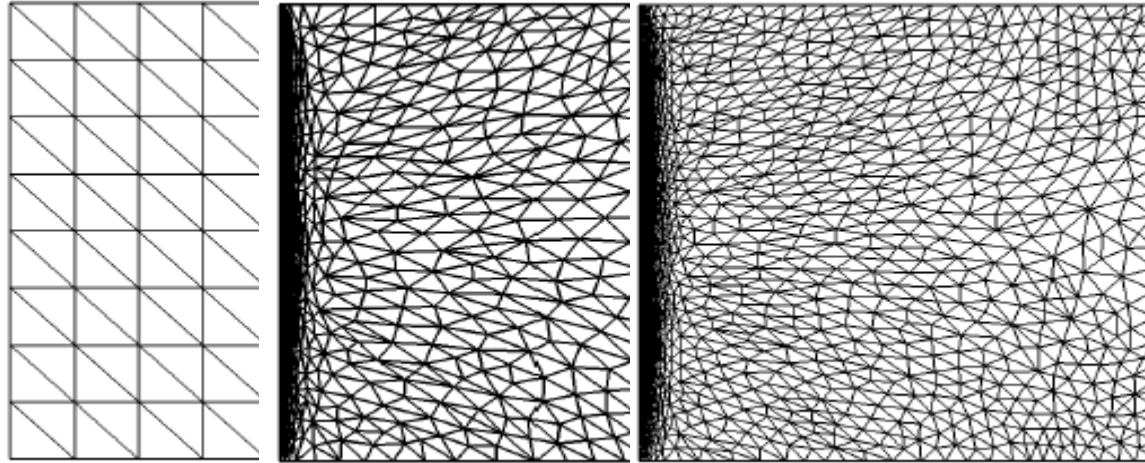
$$\|\nabla(u_h - u_h^n)\|_{L^2}^2 \approx \|\mathbf{r}^n\|_{L^2}^2$$

$$\|\mathbf{r}^n\| \leq 0.01 \left(\sum_{T \in \mathcal{T}_h} \eta_T^2 \right)^{1/2}$$

- Scaling factor $c = 0.01$

Numerical results – Steady Problems

We start from a coarse uniform **mesh** and we perform 30 adaptation steps



SOLVER:

- Conjugate Gradient (Laplace)
- GMRES (Convection – diffusion)

PRECONDITIONER:

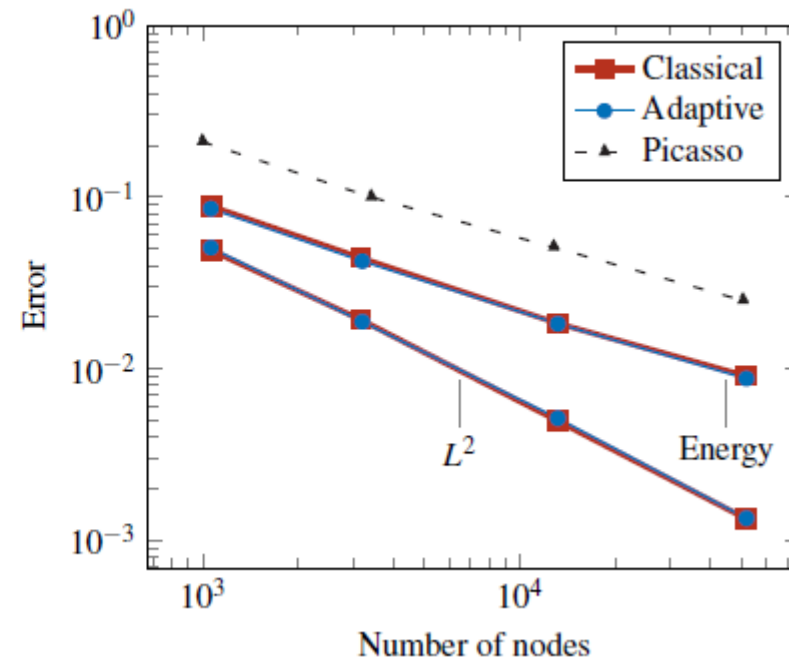
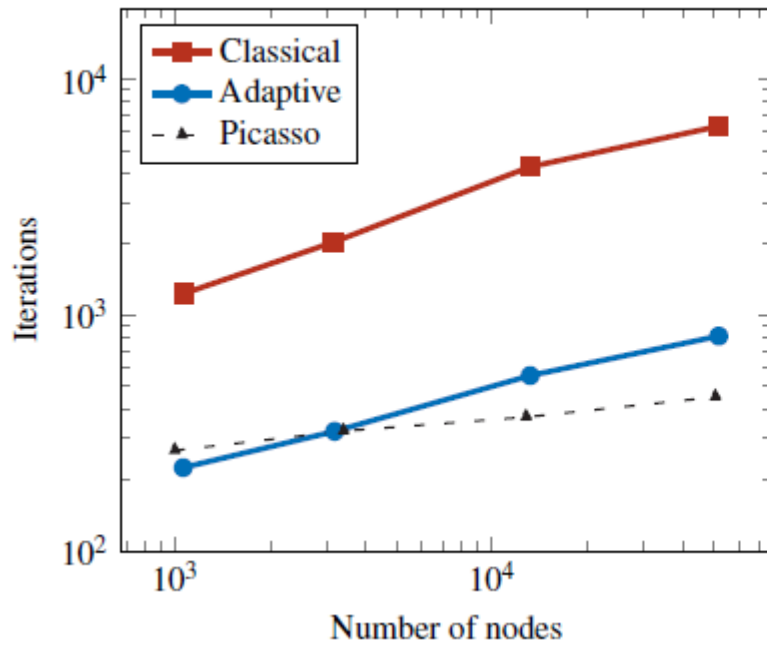
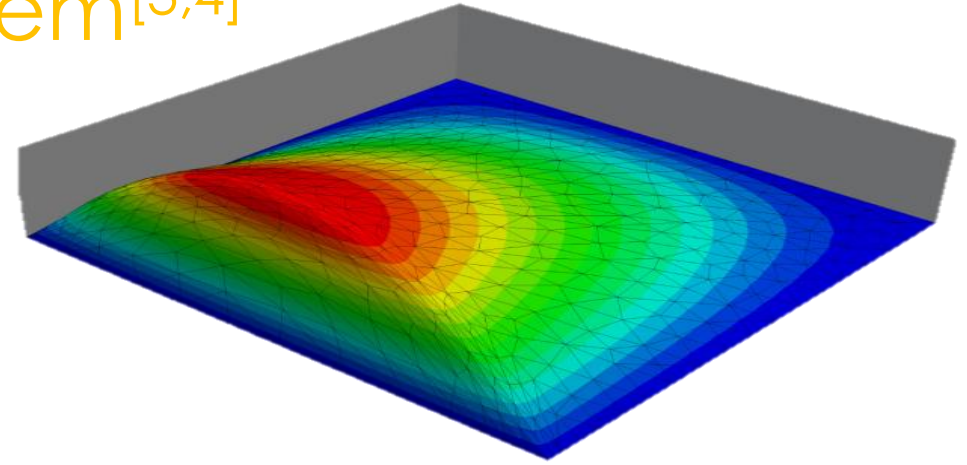
- ILU(k)
- For GMRES right preconditioner implemented

We compare the **total number** of linear **iterations** needed for the solution of all the steps

- Using a **classical** stopping criterion
- Using the proposed **adaptive** stopping criterion

Steady Problems – Laplace problem^[3,4]

$$\begin{cases} -\Delta u = f, & \text{in } \Omega, \\ u = 0, & \text{in } \Gamma. \end{cases}$$



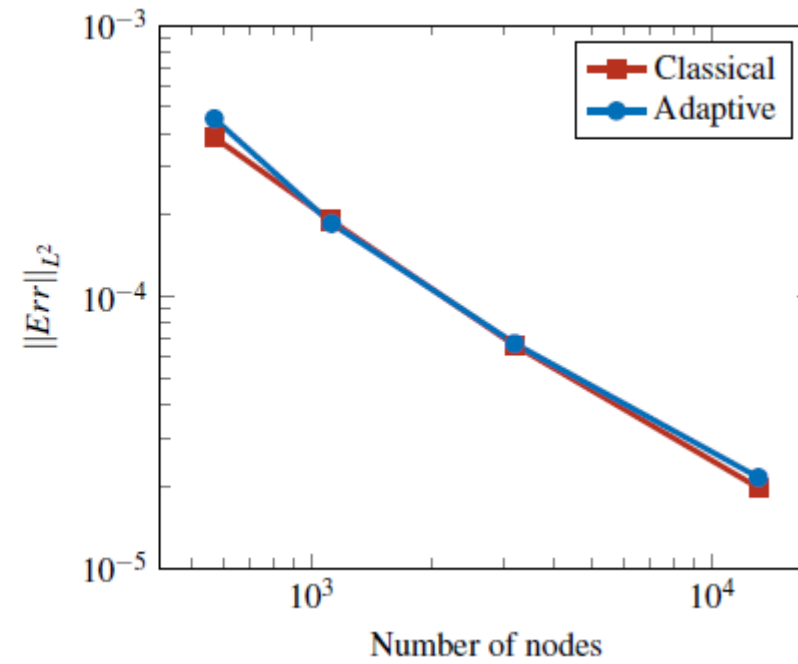
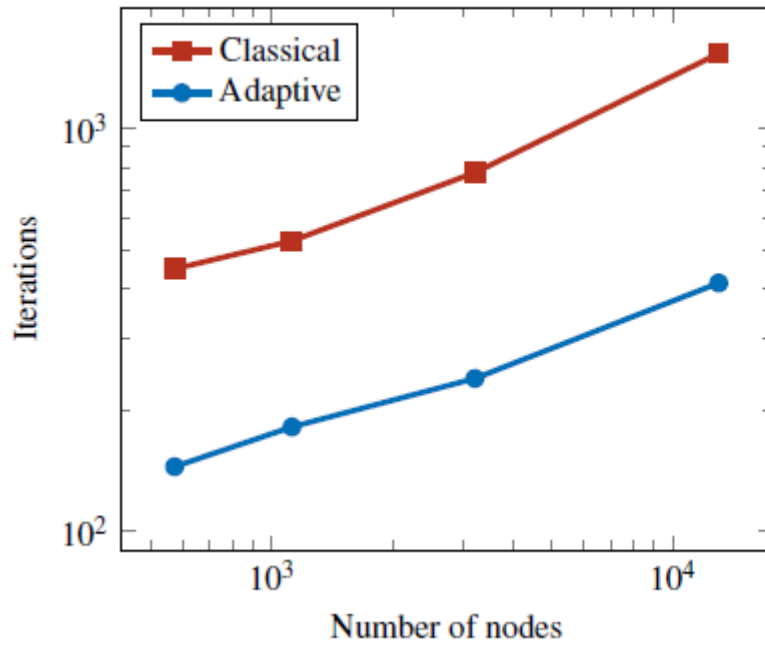
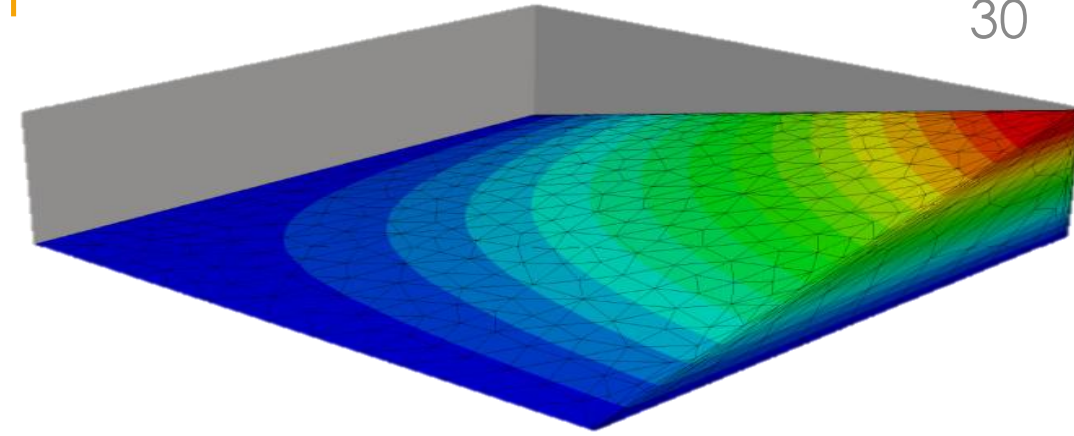
[3] Marco Picasso. A stopping criterion for the conjugate gradient algorithm in the framework of anisotropic adaptive finite elements. International Journal for Numerical Methods in Biomedical Engineering, 25(4):339–355, 2009

[4] Luca Formaggia and Simona Perotto. Anisotropic error estimates for elliptic problems. Numerische Mathematik, 94(1):67–92, 2003

Steady Problems – Convection-diffusion

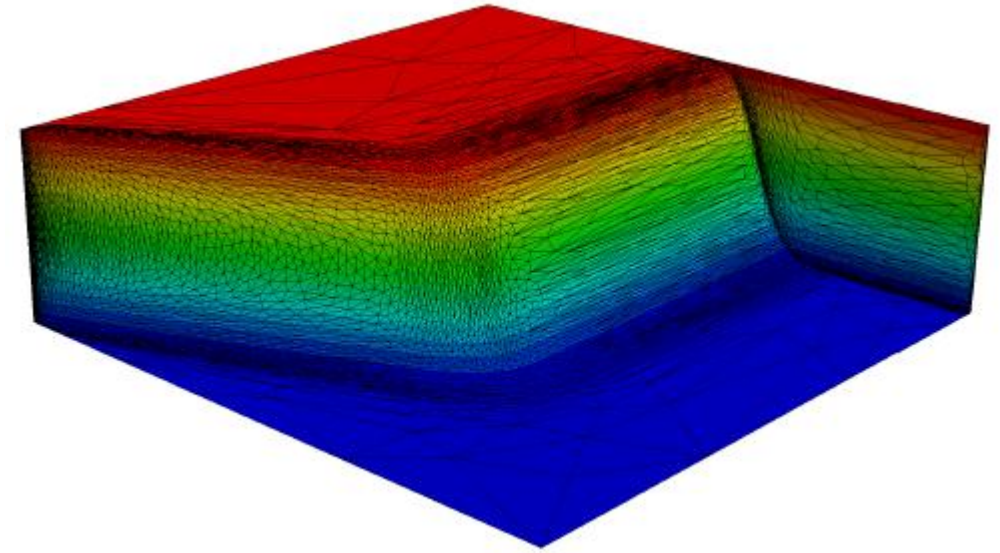
Problem equations

$$\begin{cases} -\nabla \cdot (a \nabla u) + \mathbf{v} \cdot \nabla u = f, & \text{in } \Omega \\ u = g, & \text{in } \Gamma \end{cases}$$

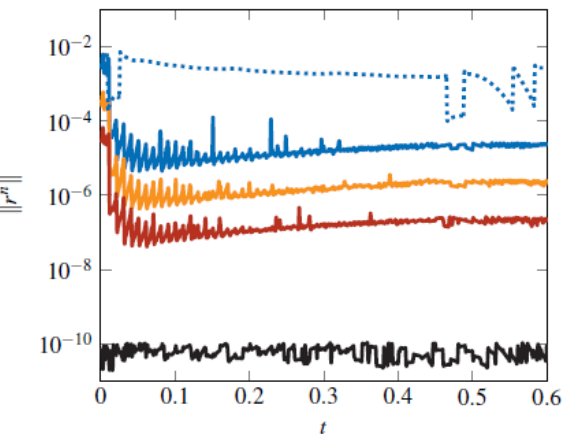


Problem equations

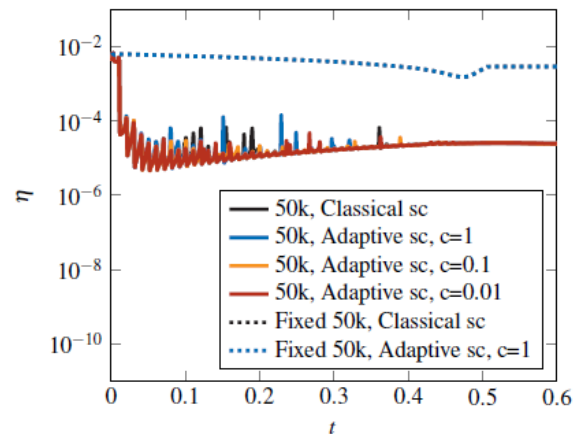
$$\begin{cases} \partial_t u(x,t) + \mathbf{v} \cdot \nabla u(x,t) - \nabla \cdot (k \nabla u(x,t)) = f & \text{in } \Omega \\ u(\cdot, 0) = u_0 & \text{in } \Omega \\ u(x,t) = g & \text{in } \Gamma \end{cases}$$



(a) Final residual.



(b) Estimated error.



Stopping criterion	Total Iterations	Ratio	CPU time Solver	CPU time reduction Solver	CPU time simulation
Classical	13633	/	158s	/	803s
Adaptive "c=0.01"	7245	1.9	91s	-42%	710s
Adaptive "c=0.1"	5615	2.4	70s	-56%	688s
Adaptive "c=1"	3882	3.5	53s	-66%	680s

$$\|\nabla(u_h - u_h^n)\|_{L^2} \leq c \left(\sum_{T \in \mathcal{T}_h} \eta_T^2 \right)^{1/2}$$

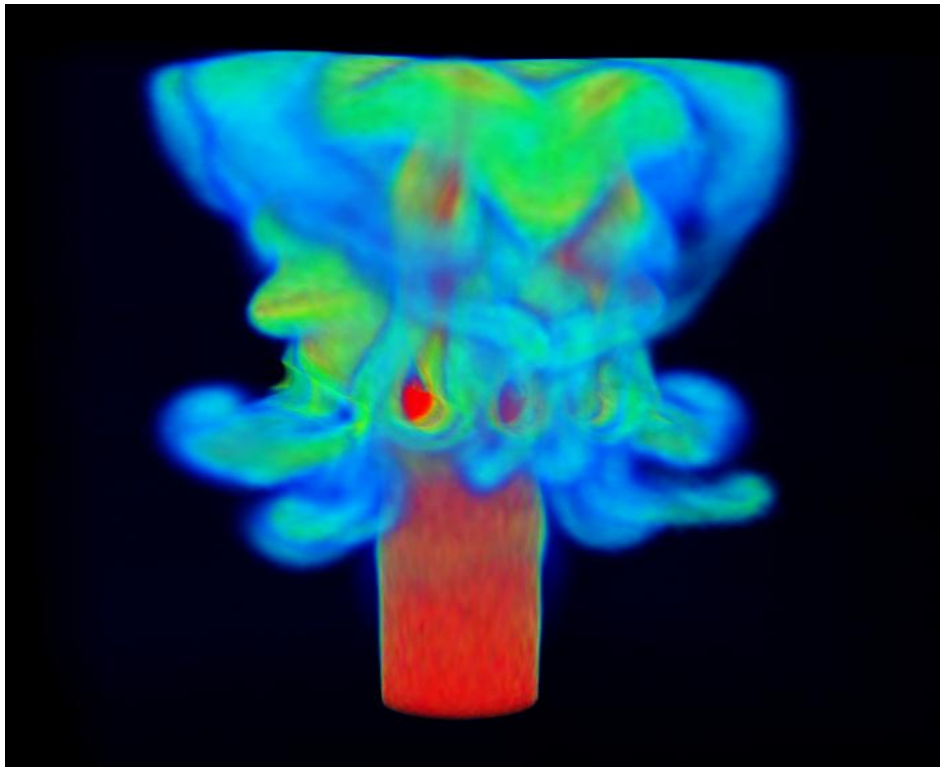
Unsteady Problems – Navier-Stokes + Thermal

$$\|\nabla(u_h - u_h^n)\|_{L^2} \leq c \left(\sum_{T \in \mathcal{T}_h} \eta_T^2 \right)^{1/2}$$

Problem equations

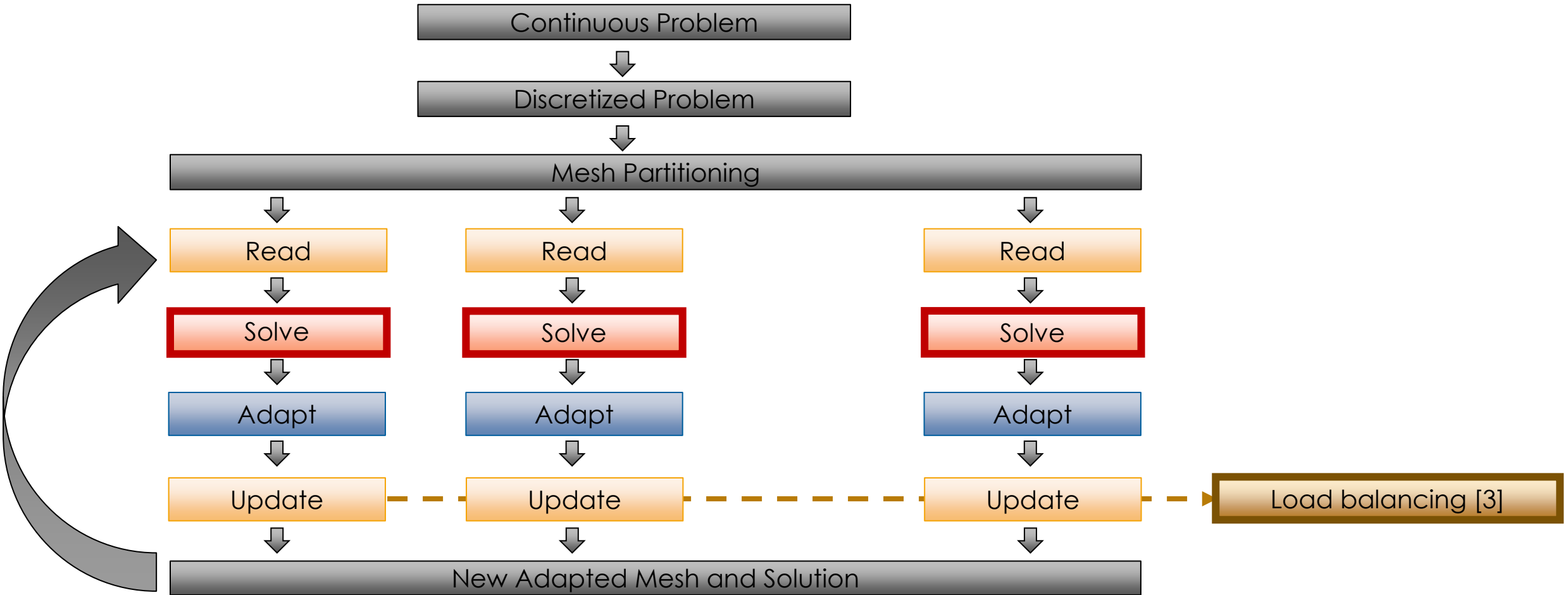
$$\begin{cases} \nabla \cdot \mathbf{u} = 0 & \text{in } \Omega \\ \rho(\partial_t \mathbf{u} + \mathbf{u} \cdot \nabla \mathbf{u}) - \nabla \cdot (2\mu \varepsilon(\mathbf{u}) - p \mathbf{I}_d) = \rho_0 \beta (T - T_0) \mathbf{g} & \text{in } \Omega \\ \rho C_p (\partial_t T + \mathbf{u} \cdot \nabla T) - \nabla \cdot (\lambda \nabla T) = f & \text{in } \Omega \end{cases}$$

→ ~ 40% CPU time saving



Stopping criterion	Total Iterations	Ratio	CPU time Solver	CPU time reduction Solver	CPU time simulation
Classical	609922	/	37h	/	41h
Adaptive "c=0.1"	107846	5.7	23h	-38%	28h

AFEM Framework – Load balancing



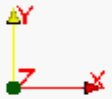
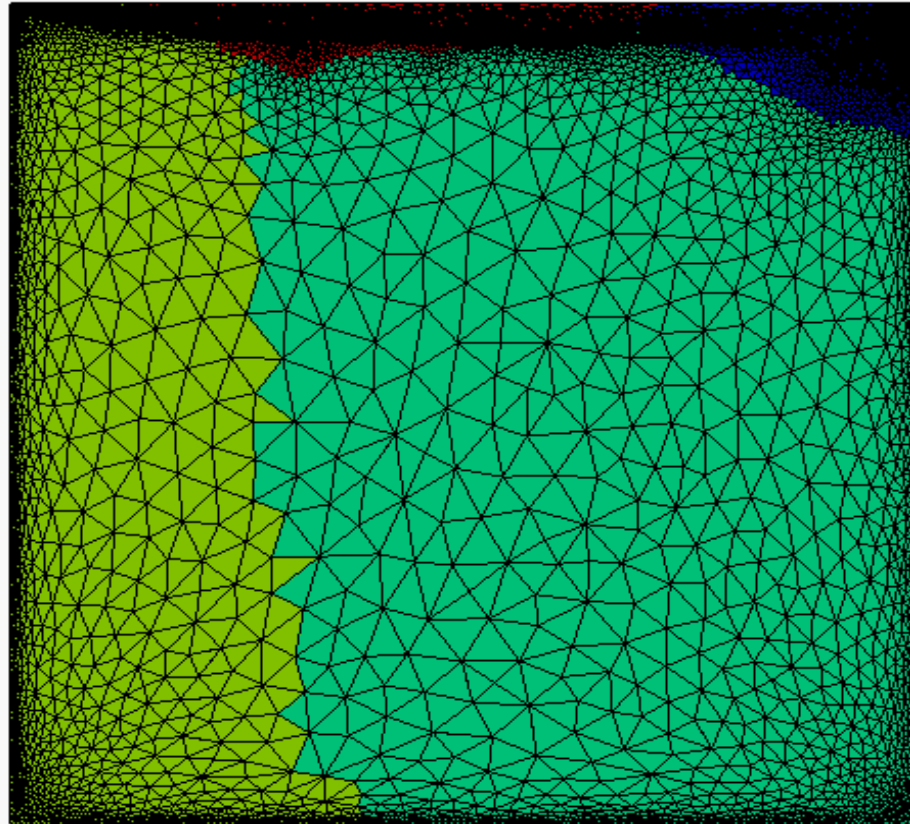
[1] G. Manzinali, E. Hachem, Y. Mesri, Adaptive stopping criterion for iterative linear solvers combined with anisotropic mesh adaptation, application to convection-dominated problems, CMAME, 2018

[2] Bazile, A., Hachem, E., Larroya-Huguet, J. C., Mesri, Y. Variational Multiscale error estimator for anisotropic adaptive fluid mechanic simulations: Application to convection-diffusion problems, CMAME, 331, 94-115, 2018.

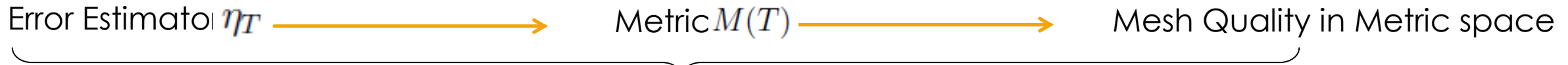
[3] Y. Mesri, Predictive load balancing for parallel anisotropic mesh adaptation applications, preprint, 2018

Dynamic load balancing (lid-driven cavity)

Load balancing based on local topological mesh repartitioning

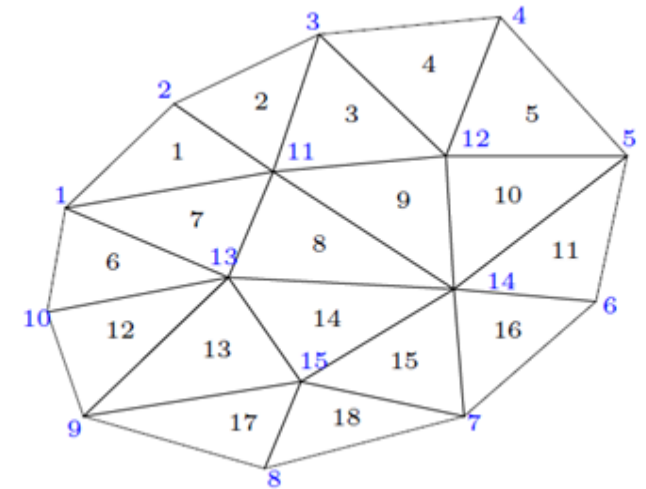
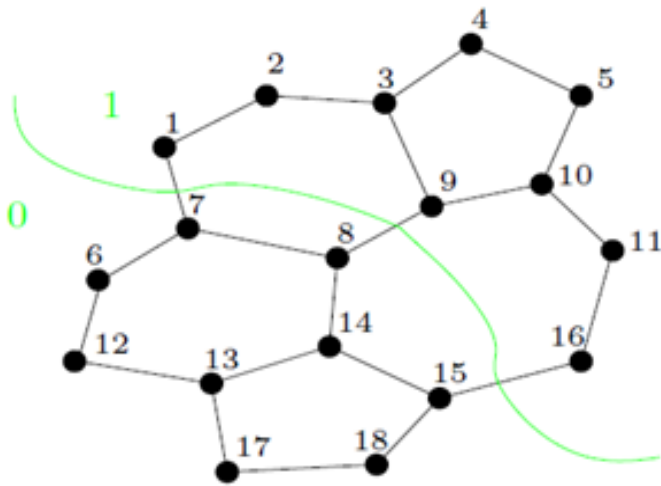


Estimate the expected dynamic workload



$$q(T) = C_0 \frac{(Volume)(T)_{M(T)}}{h_{M(T)}^d}$$

Weights the mesh/graph entities for repartitioning



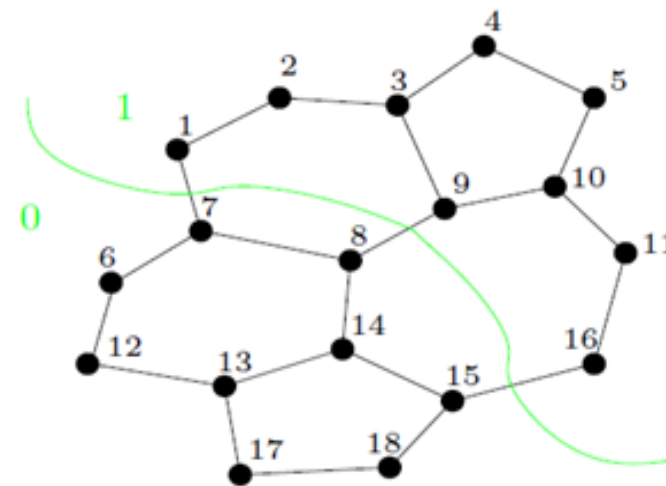
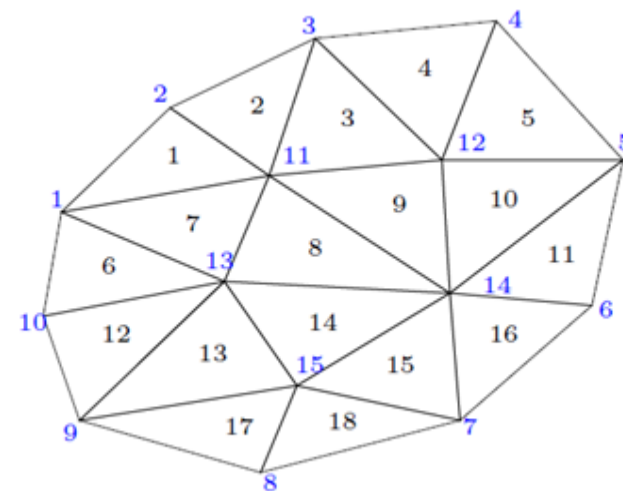
Predictive load balancing

1
$$q(T) = C_0 \frac{(\text{Volume})(T) M(T)}{h_{M(T)}^d}$$

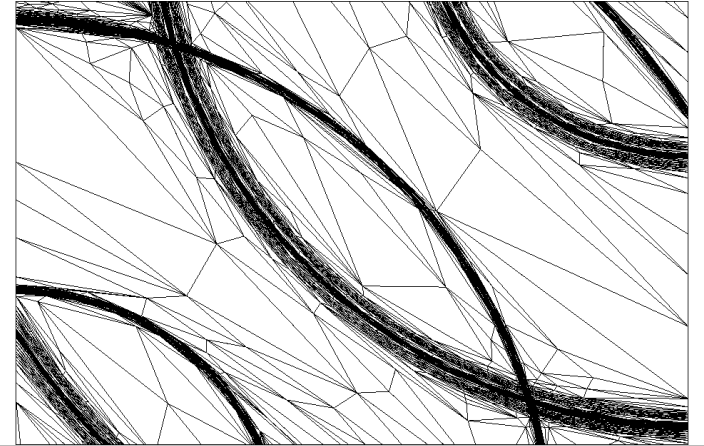
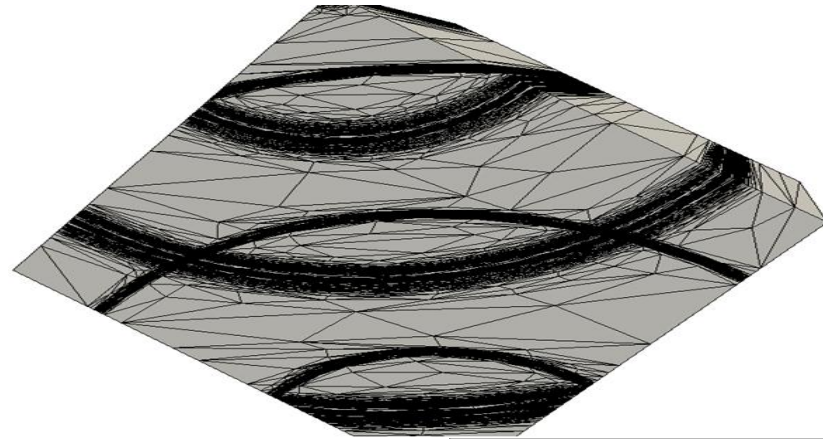
2
$$w(v) = \frac{1}{q(T)}$$

3
$$w(u, v) = \frac{1}{2q(S)} + \frac{1}{2q(T)}$$

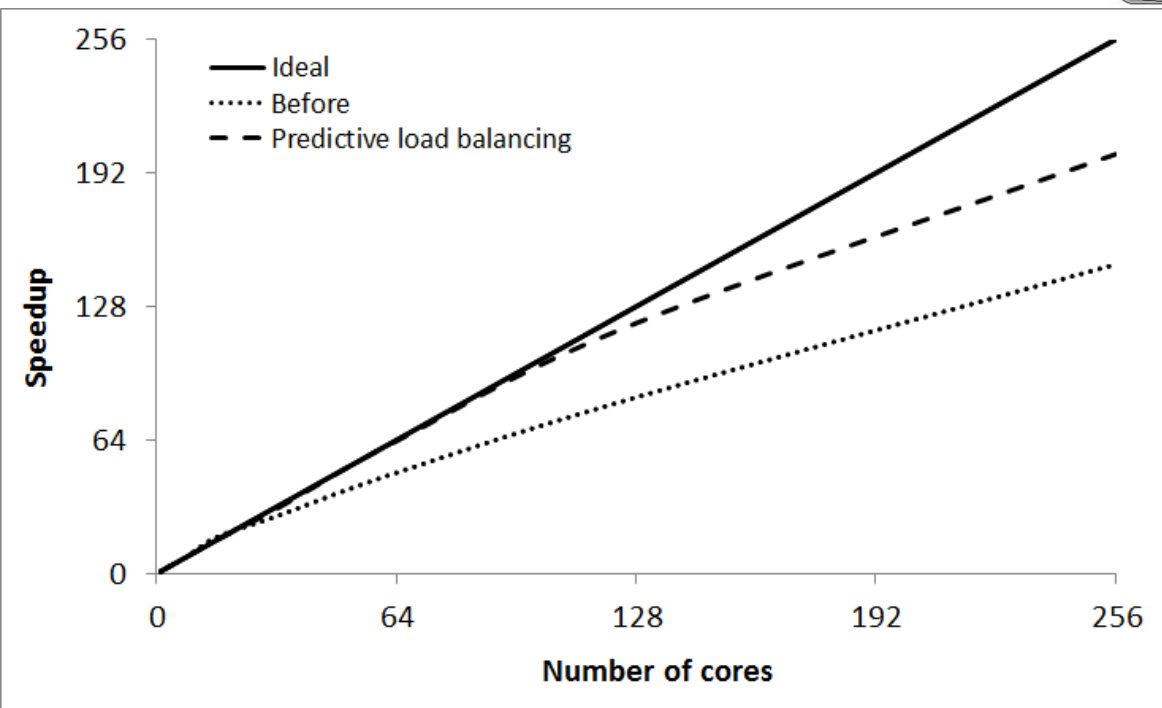
4
$$F(W, A, m) := \max_{p \in V(A)}(t_p) + \max_{p \in V(A)}(c_p)$$



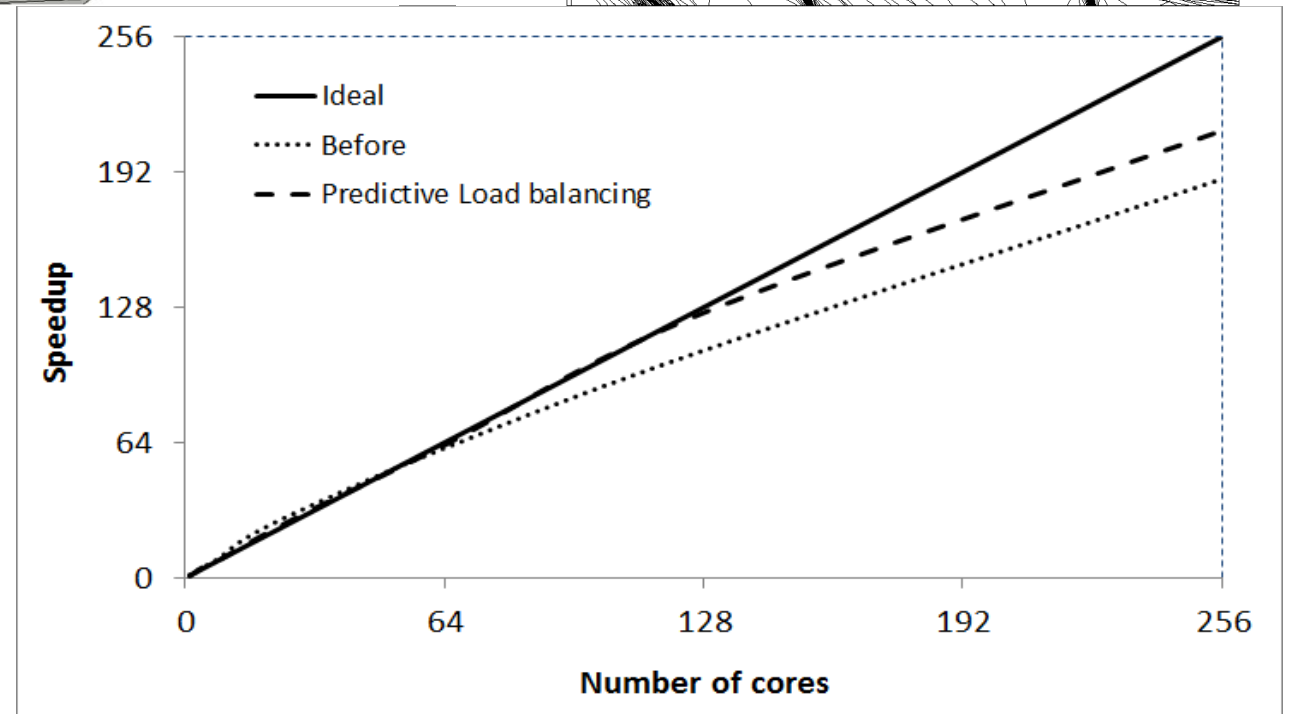
Predictive load balancing



Y. Mesri, Parallel High-Reynolds Incompressible Flow with Adaptive Anisotropic Meshing, submitted



3D test case

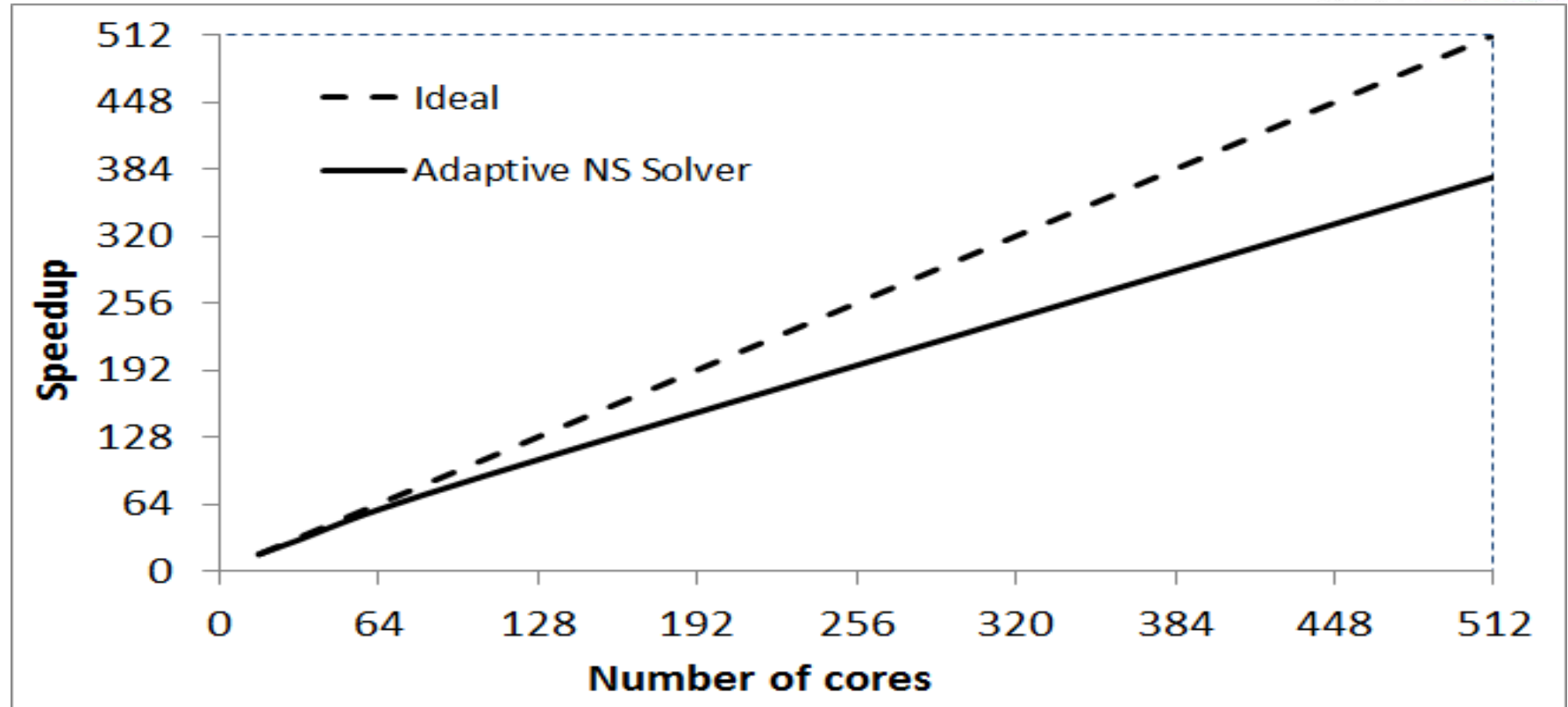
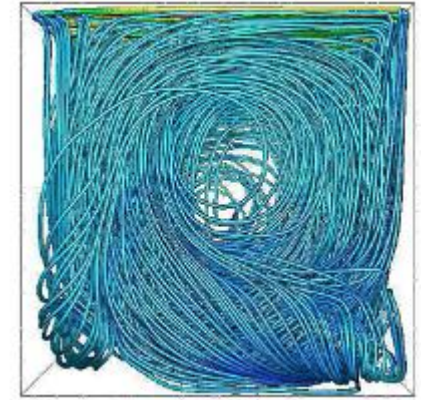
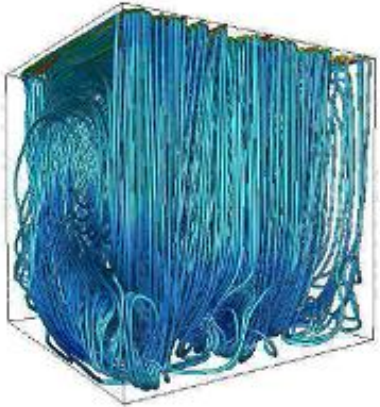


2D test case

Parallel NS with predictive load balancing

3D lid-driven cavity

30M elements
NS Incompressible
Re = 3200



Potential Collaboration topics?

Solve over 100 billion unknowns system

Methods

- Numerical Methods and their implementation
- Experimental prototyping and calibration
- Data analytics

Technology

- Cloud computing
- HPC and big data processing
- Artificial Intelligence/DL/ML

Applications

- Multi-phase flows
- Fluid Structure Interaction
- Heat transfer

Targets new applications

- Digital Health
- Mobility
- ...

- Système d'équations aux dérivées partielles

$$\mathcal{A}(u) = f$$

- Méthode numérique

$$\mathcal{A}_h(u_h) = f_h$$

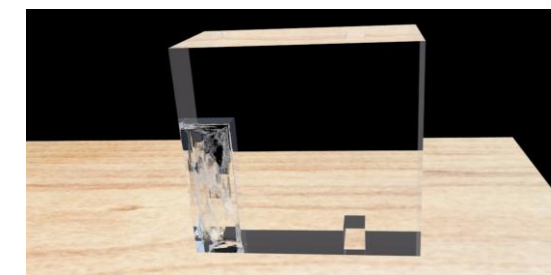
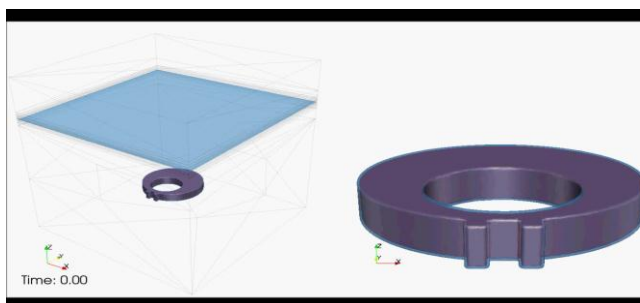
- Résolution itérative

$$A^{k-1}U^{k,i} = F^{k-1} - R^{k-1,i},$$

le vecteur $U^{k,i}$ est une représentation algébrique de u_h à l'itération non-linéaire k et linéaire i



(3) Over 262 144 JuQUEEN cores



THANK YOU FOR YOUR
ATTENTION